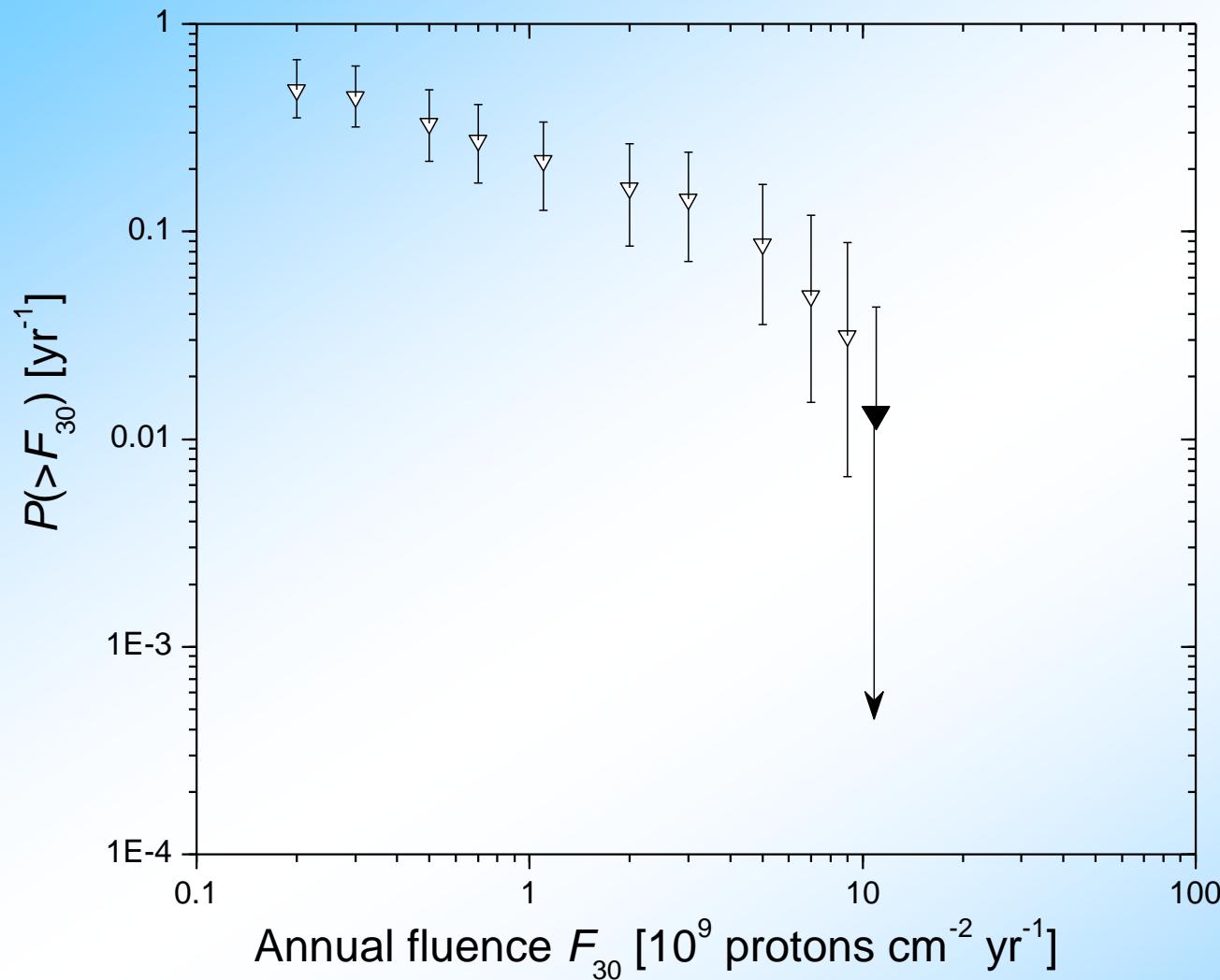


OCCURRENCE OF EXTREME SEP EVENTS ON DIFFERENT TIME SCALES

Ilya Usoskin

University of Oulu, Finland

Direct data: since 1950s



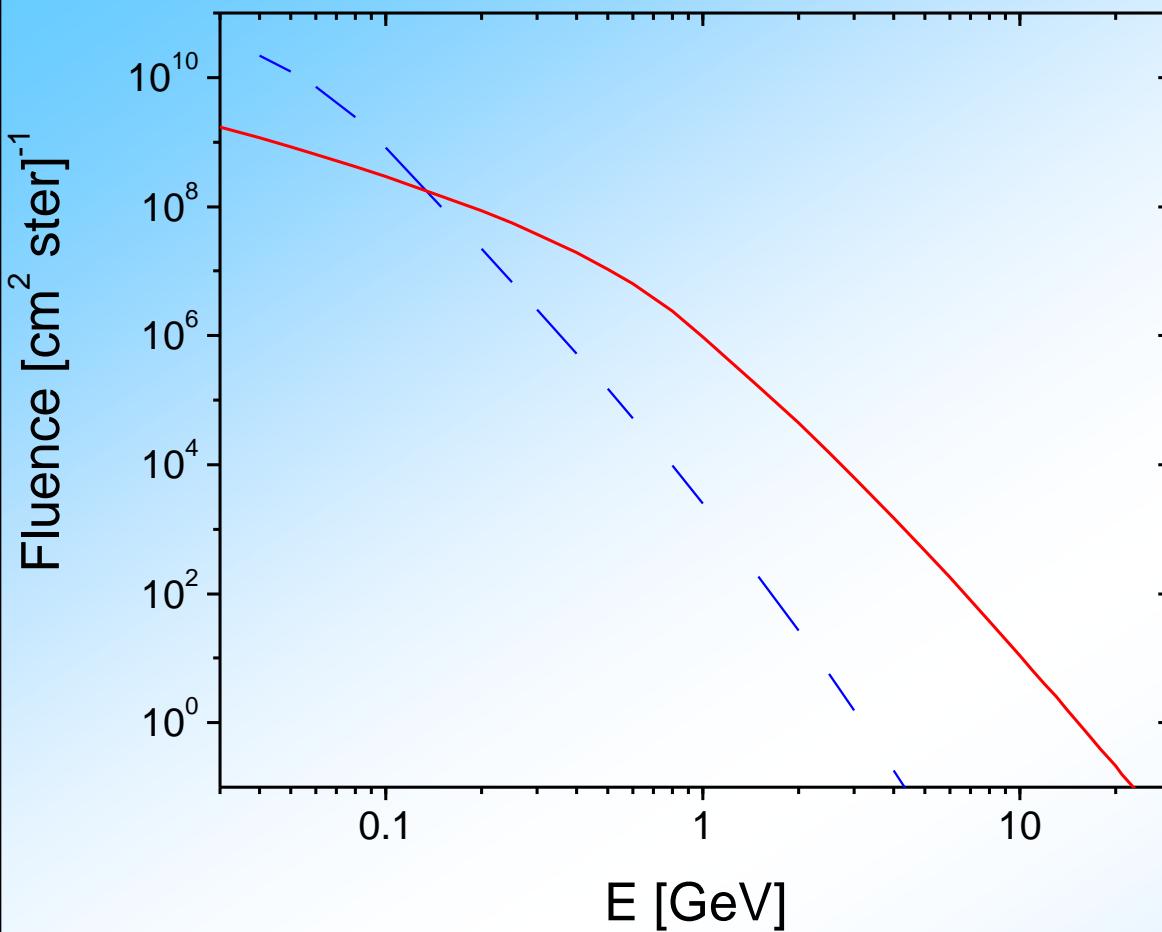
Shea & Smart (1990, 2012), Reedy (2012):
No events with $F_{30} > 10^{10} \text{ cm}^{-2}$ since 1956.

Cosmogenic radionuclides: last 11 millennia

Data series used

- **IntCal09** $\Delta^{14}\text{C}$ global series: 11000 BC – 1900 AD, 5-yr time resolution (Reimer et al. 2009).
- **SB93** $\Delta^{14}\text{C}$ global annual series: 1511 – 1900 AD (Stuiver & Braziunas 1993).
- **Dye3** ^{10}Be Greenland annual series: 1424–1985 AD (Beer et al. 1990).
- **NGRIP** ^{10}Be Greenland annual series: 1389–1994 AD (Berggren et al. 2009).
- **SP** ^{10}Be South Pole Antarctic series: 850–1950 AD, quasi-decadal (Raisbeck et al. 1990; Bard et al. 1997).
- **DF** ^{10}Be Dome Fuji Antarctic series: 695–1880 AD, quasi-decadal (Horiuchi et al. 2008).
- **GRIP** ^{10}Be Greenland series: 7380 BC–1640 AD, quasi-decadal (Yiou et al. 1997; Vonmoos et al. 2006).
- ^{14}C (Miyake et al., 2012, 2013)

SPE scenaria



SPE56:

23-Feb-1956 – hard spectrum

NM: 4000% at Leeds NM

$F_{30} = 10^9 \text{ cm}^{-2}$ (Shea & Smart, 1990)

$Q_{^{10}\text{Be}} = 7.5 \times 10^4 \text{ at/cm}^2$ (intermediate mixing)

$Q_{^{14}\text{C}} = 2.9 \times 10^6 \text{ at/cm}^2$ (global)

SPE72:

04-Aug-1972 – soft spectrum

NM: 10% at Oulu NM

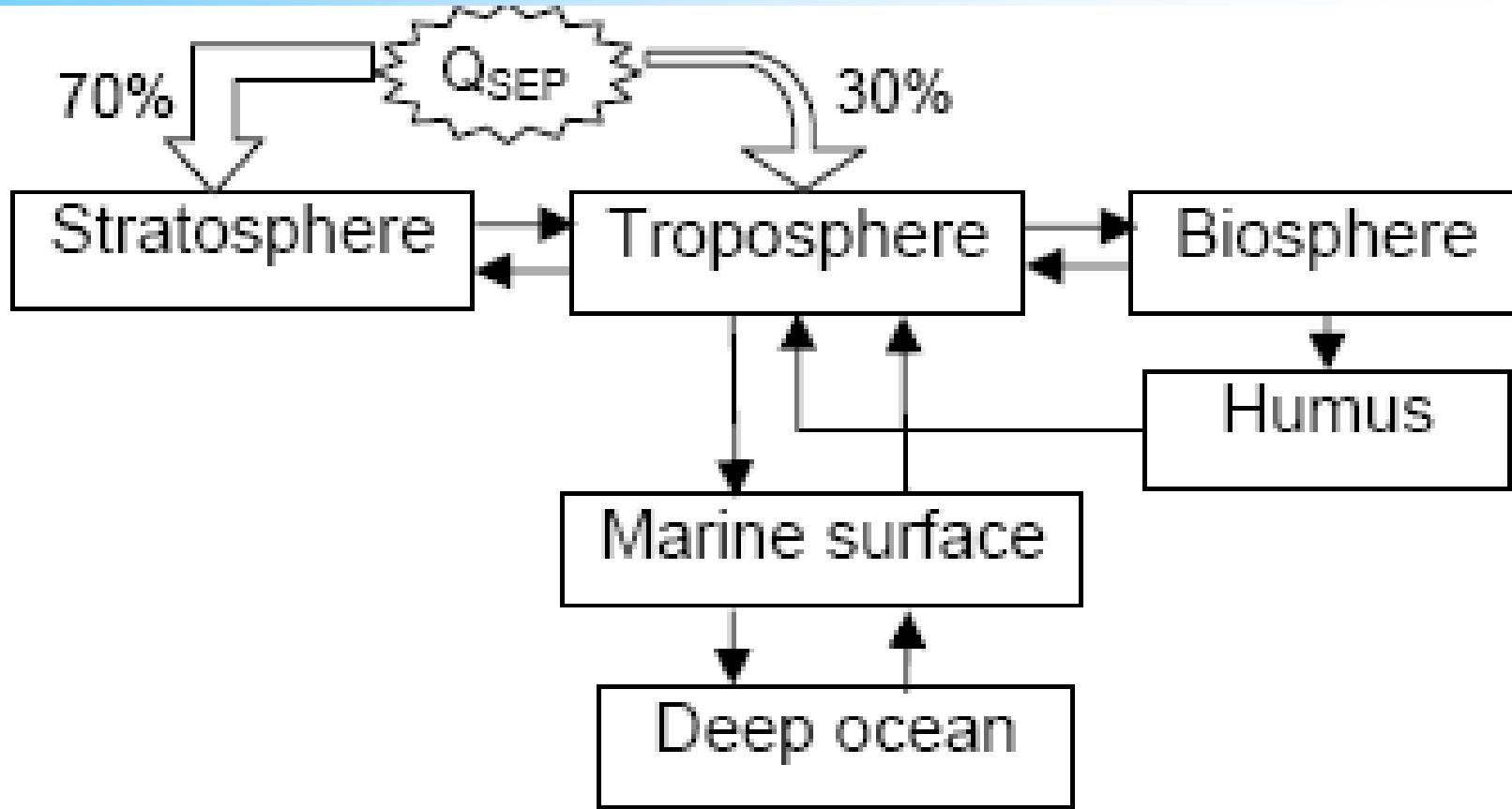
$F_{30} = 5 \times 10^9 \text{ cm}^{-2}$

$Q_{^{10}\text{Be}} = 1.1 \times 10^4 \text{ at/cm}^2$ (intermediate mixing)

$Q_{^{14}\text{C}} = 3.1 \times 10^5 \text{ at/cm}^2$ (global)

$^{14}\text{C} / {^{10}\text{Be}} \rightarrow F_{200}$, not F_{30} , conversion is a matter of spectrum. Soft-spectrum event may be missing in the cosmogenic nuclide data.
The same isotope signal requires 40X greater F_{30} in SPE72 than in SPE56,

Carbon cycle



775 AD: model vs. data

SEP → production → $Q_{^{14}\text{C}}$

(Kovaltsov et al., 2012)

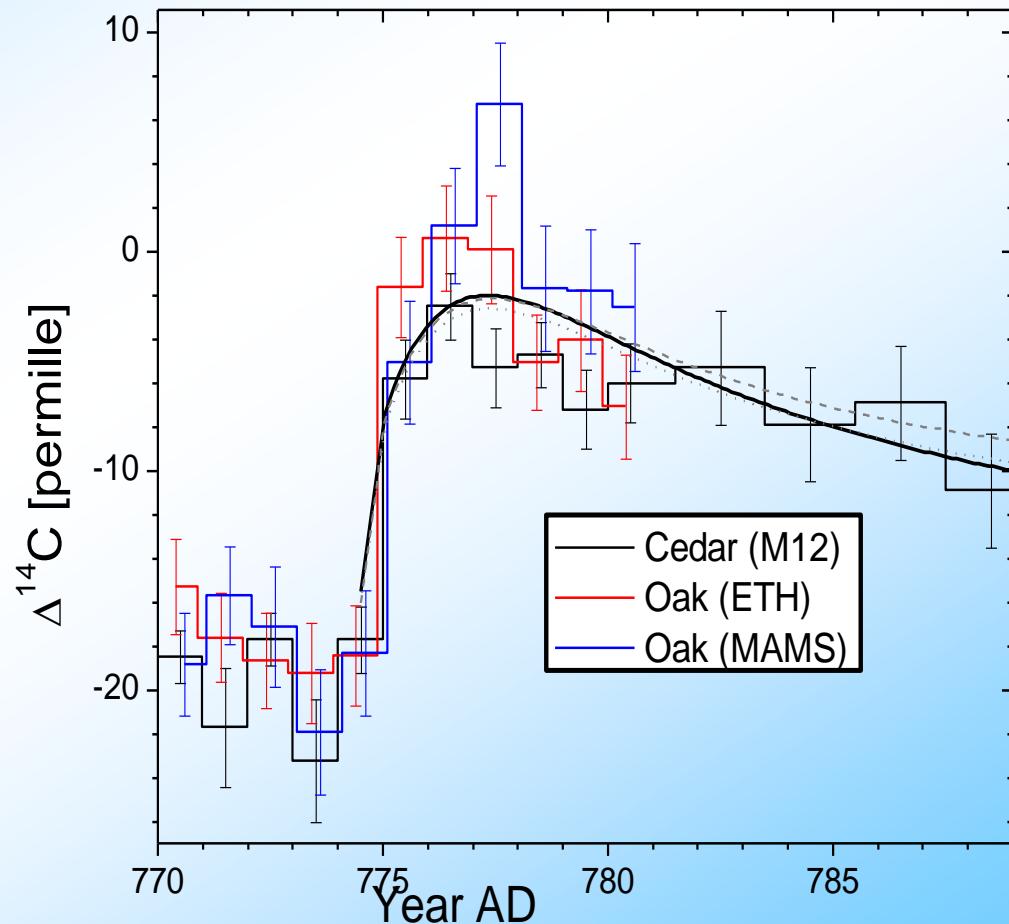
$Q \rightarrow$ carbon cycle $\rightarrow \Delta^{14}\text{C}$

5-box model (Damon & Peristykh, 2004)

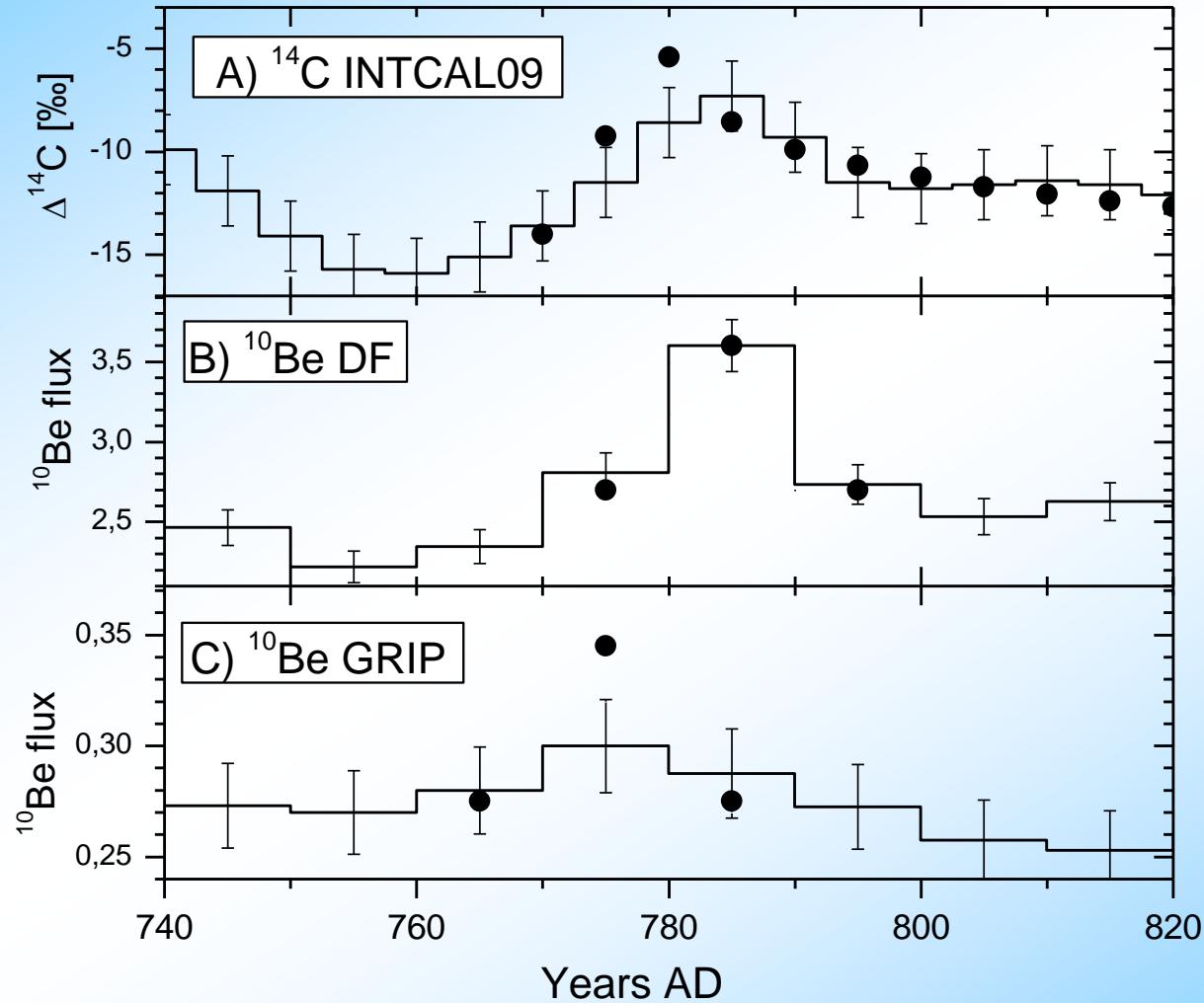
Response for SPE56 is:

Peak – 0.2-0.35 ‰ (errors ~2 ‰),
FWHM~20-30 yrs, rise time 0-10 yrs.

Fit of 45 SPE56 ($F_{30}=4.5 \times 10^{10} \text{ cm}^{-2}$) →



775 AD – other data



Candidates from annual series (600 yrs)

| | | | |
|--------------|-------|------------|-------------------------------------|
| • 1460-1462: | NGRIP | $F_{30} =$ | $1.5 \cdot 10^{10} \text{ cm}^{-2}$ |
| | Dye3 | | $1 \cdot 10^{10}$ |
| • 1505 | Dye3 | | $1.3 \cdot 10^{10}$ |
| • 1719 | NGRIP | | $1 \cdot 10^{10}$ |
| • 1810 | NGRIP | | $1 \cdot 10^{10}$ |

* **4 events** with $F_{30}=1-1.5 \cdot 10^{10} \text{ cm}^{-2}$ over 600 years

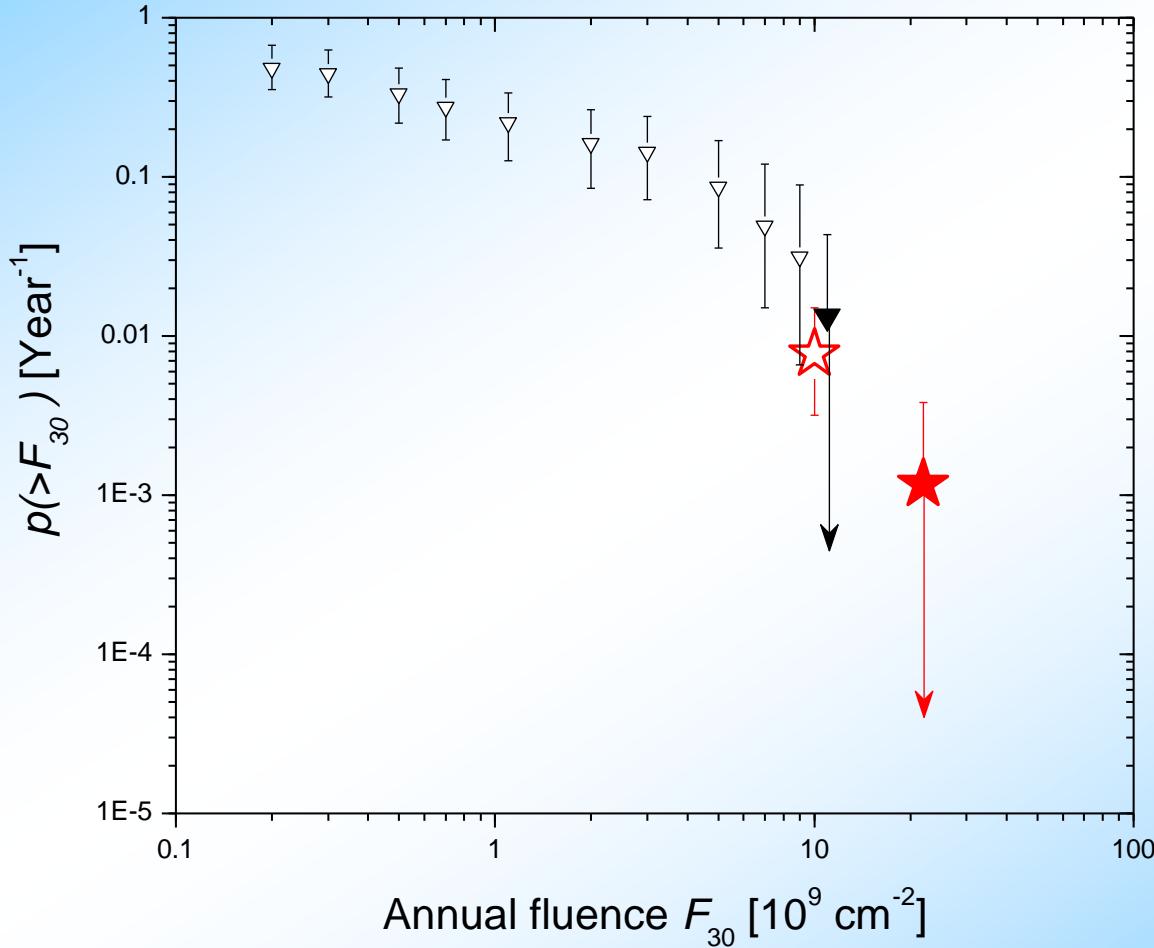
* **no events** with $F_{30}>2 \cdot 10^{10} \text{ cm}^{-2}$ over 600 years

Thus:

$$p=0.0077(^{+0.0073}_{-0.0045}) \text{ yr}^{-1} - 1/130 \text{ yr for } F_{30}<2 \cdot 10^{10} \text{ (NB: not } 4/600=1/150 \text{ yr !)}$$

$$p=0 - 0.0027 \text{ yr}^{-1} - \text{rarer than } 1/400 \text{ yr for } F_{30}>2 \cdot 10^{10} \text{ (median } 1/850 \text{ yr}^{-1})$$

SPEs: 600 years of data



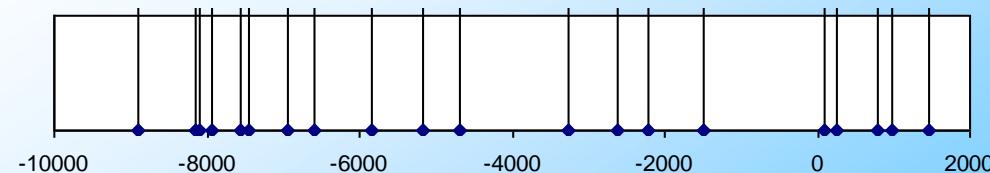
Candidates from rougher series

| | | |
|-----------|-------------|-------------------------------------|
| • 8910 BC | IntCal09 | 2.0×10^{10} |
| • 8155 BC | IntCal09 | 1.3×10^{10} |
| • 8085 BC | IntCal09 | 1.5×10^{10} |
| • 7930 BC | IntCal09 | 1.3×10^{10} |
| • 7570 BC | IntCal09 | 2.0×10^{10} |
| • 7455 BC | IntCal09 | 1.5×10^{10} |
| • 6940 BC | IntCal09 | 1.1×10^{10} |
| • 6585 BC | IntCal09 | 1.7×10^{10} |
| • 5835 BC | IntCal09 | 1.5×10^{10} |
| • 5165 BC | GRIP | 2.4×10^{10} |
| • 4680 BC | IntCal09 | 1.6×10^{10} |
| • 3260 BC | IntCal09 | 2.4×10^{10} |
| • 2615 BC | IntCal09 | 1.2×10^{10} |
| • 2225 BC | IntCal09 | 1.2×10^{10} |
| • 1485 BC | IntCal09 | 2.0×10^{10} |
| • 95 AD | GRIP | 2.6×10^{10} |
| • 265 AD | IntCal09 | 2.0×10^{10} |
| • 780 AD | IntCal09/DF | $2-5 \times 10^{10}$ |
| • 990 AD | M13 | 2.5×10^{10} |
| • 1455 AD | SP | 7.0×10^{10} overestimate?? |

Statistics for 11400 years:

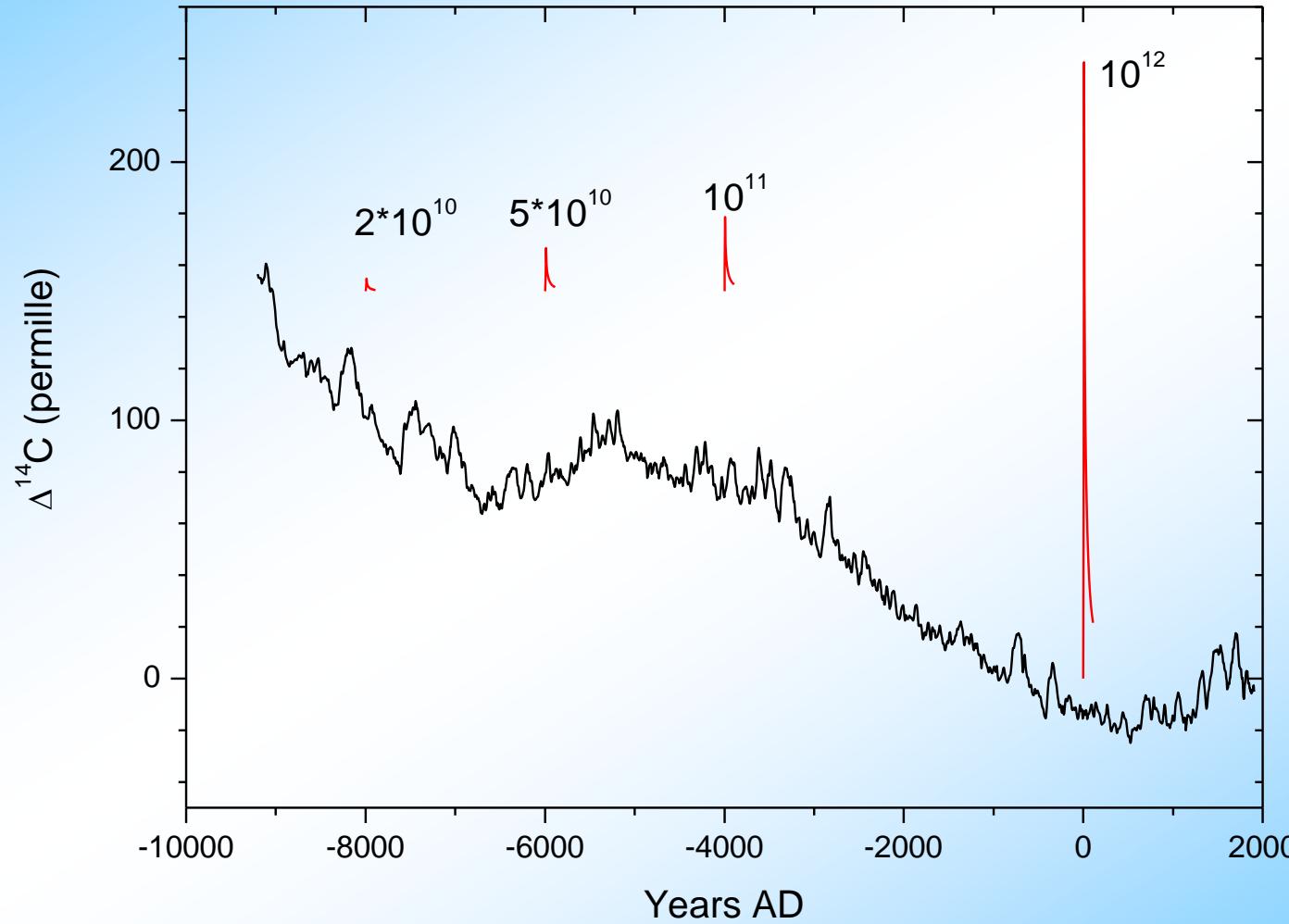
20 events $F_{30} = (1-3) \times 10^{10} \text{ cm}^{-2}$

no events with $F_{30} > 5 \times 10^{10} \text{ cm}^{-2}$

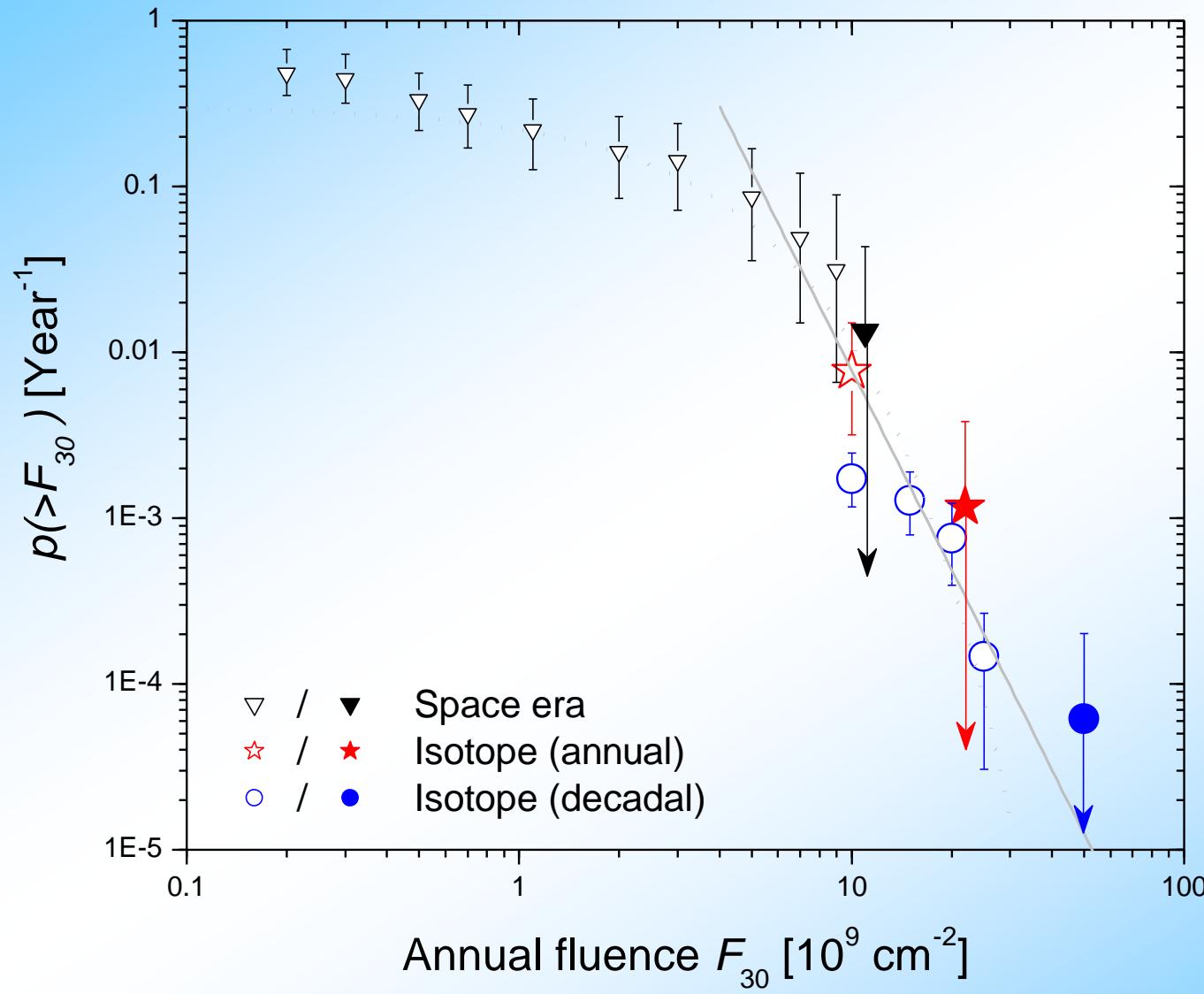


7.0*10¹⁰ overestimate??

Events to look for in $\Delta^{14}\text{C}$



SPEs: all data

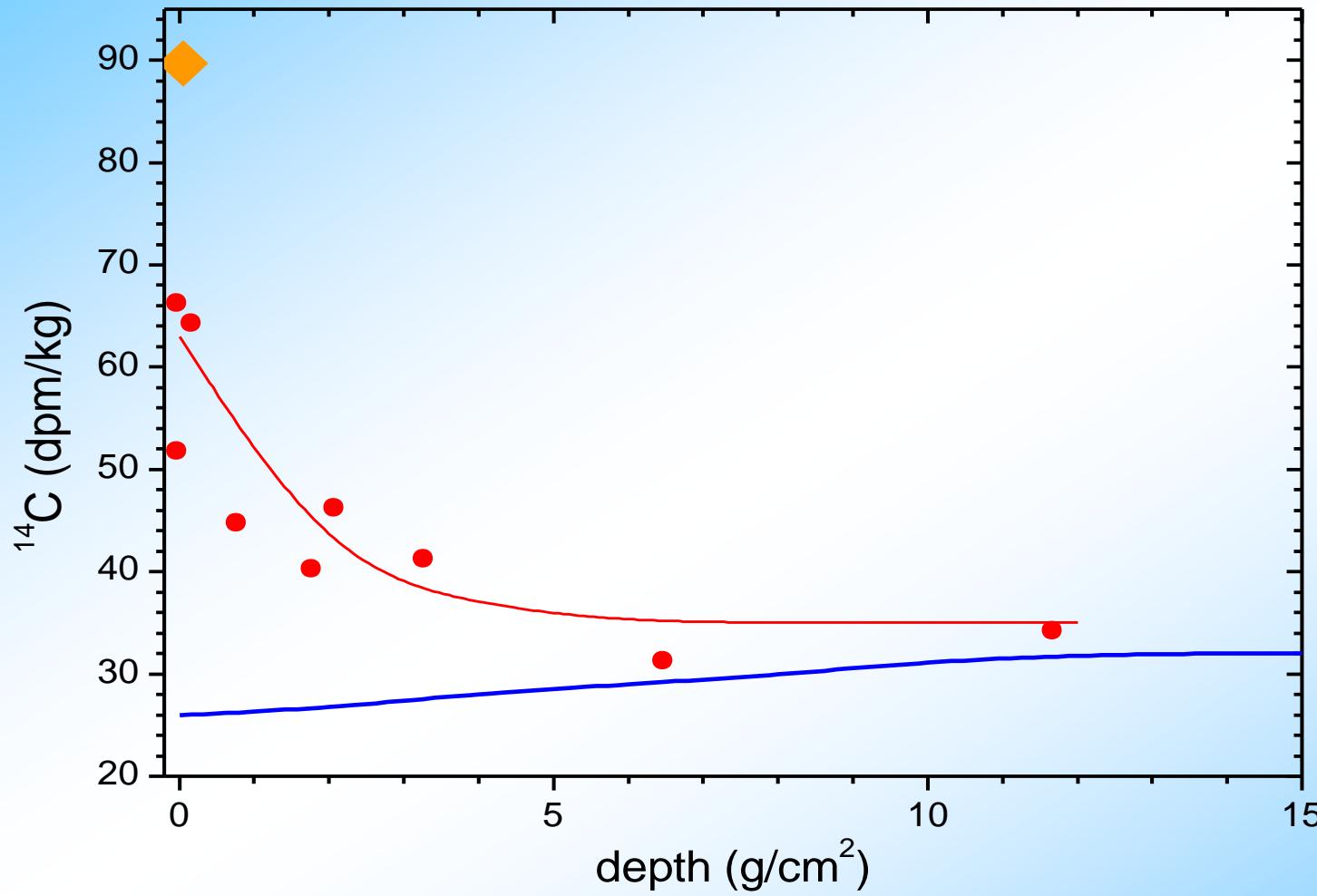


Subconclusions

- Four potential candidates with $F_{30} = (1 \div 1.5) * 10^{10}$ cm⁻² and no events with $F_{30} > 2 * 10^{10}$ cm⁻² identified since 1400 AD in the annually resolved ¹⁰Be data.
- For the Holocene, 20 SPEs with $F_{30} = (1 \div 3) * 10^{10}$ cm⁻² are found in the ¹⁴C and ¹⁰Be data and clearly no event with $F_{30} > 5 * 10^{10}$ cm⁻².
- On average, extreme SPEs contribute about 10% to the total SEP flux.
- Practical limits are: $F_{30} \approx 1$, $2 \div 3$, and $5 * 10^{10}$ cm⁻² for the occurrence probability $\approx 10^{-2}$, 10^{-3} and 10^{-4} year⁻¹, respectively.
- BUT: uncertainty of conversion $F_{200} \rightarrow F_{30}$

Cosmogenic radionuclides in lunar rocks: 1 Myr

Lunar/meteoritic samples



^{14}C activity in a lunar sample 68815 (Jull et al., 1998).

Lunar rock data

Table 1. Assessments of the parameters of OPDF from different cosmogenic radionuclide data in lunar rocks. Columns correspond to the nuclide, reference to the original data, the measured mean annual fluence F^* (10^9 protons/cm 2 /yr), and the corresponding best-fit parameters α and β (10^{-9} cm 2 yr) with the 90% confidence intervals (see text).

| # | Nuclide | Reference | F^* | α | β |
|----|---------------------------------|-----------------------------------|-------|-----------------|-------------------|
| 1 | ^{14}C | (Jull <i>et al.</i> , 1998) | 1.33 | 2.64 ± 0.21 | 0.328 ± 0.037 |
| 2 | ^{41}Ca | (Fink <i>et al.</i> , 1998) | 1.77 | 1.67 ± 0.03 | 0.134 ± 0.002 |
| 3 | ^{81}Kr | (Reedy, 1999) | 1.51 | 2.01 ± 0.02 | 0.202 ± 0.003 |
| 4 | ^{36}Cl | (Nishiizumi <i>et al.</i> , 2009) | 1.45 | 2.16 ± 0.02 | 0.232 ± 0.003 |
| 5 | ^{26}Al | (Kohl <i>et al.</i> , 1978) | 0.79 | N/A | N/A |
| 6 | ^{26}Al | (Grismore <i>et al.</i> , 2001) | 1.74 | 1.69 ± 0.01 | 0.137 ± 0.001 |
| 7 | $^{10}\text{Be}/^{26}\text{Al}$ | (Nishiizumi <i>et al.</i> , 1988) | 1.10 | 6.93 ± 0.14 | 1.19 ± 0.03 |
| 8 | $^{10}\text{Be}/^{26}\text{Al}$ | (Michel, Leya, and Borges, 1996) | 0.76 | N/A | N/A |
| 9 | $^{10}\text{Be}/^{26}\text{Al}$ | (Fink <i>et al.</i> , 1998) | 1.01 | N/A | N/A |
| 10 | $^{10}\text{Be}/^{26}\text{Al}$ | (Nishiizumi <i>et al.</i> , 2009) | 0.76 | N/A | N/A |
| 11 | ^{53}Mn | (Kohl <i>et al.</i> , 1978) | 0.79 | N/A | N/A |

Fluence is averaged over the isotope's life time (production-vs-decay balance) – no time resolution.

Earlier estimate

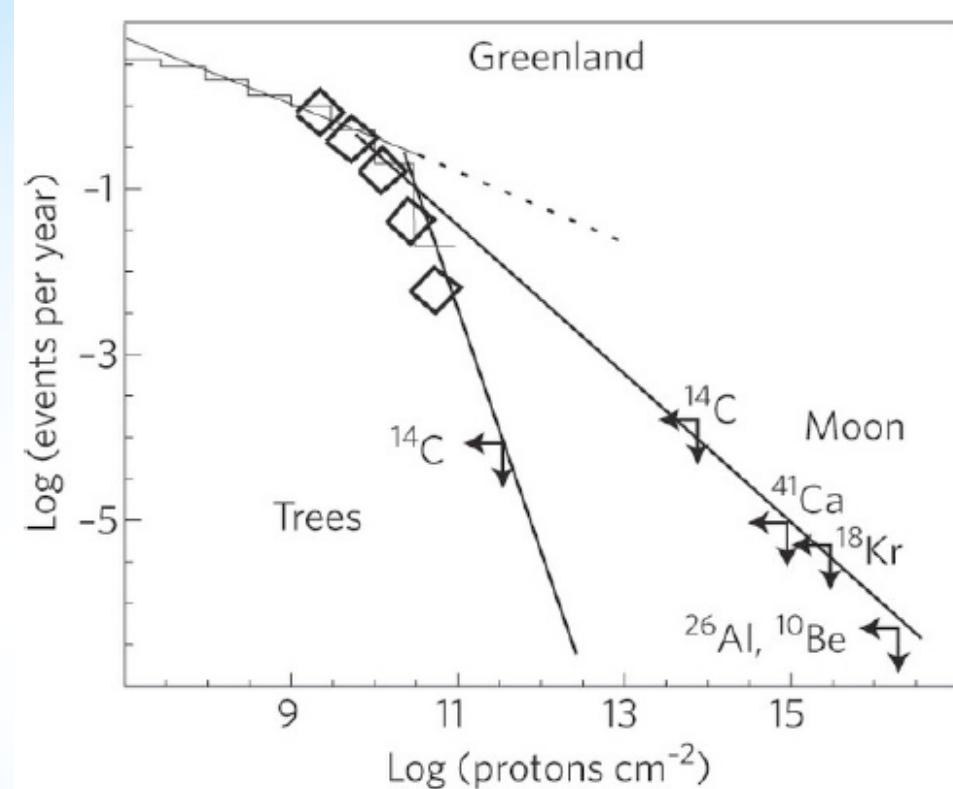
^{14}C :

$$\text{P} \sim 10^{-4} \text{ yr}^{-1} = 1/\tau (\sim 6 \text{ kyr}),$$
$$F_{30} \sim 10^{13} \text{ p/cm}^2/\text{yr} = 10^9 * \tau$$

By definition, $\alpha=1$.

Reedy (1996):

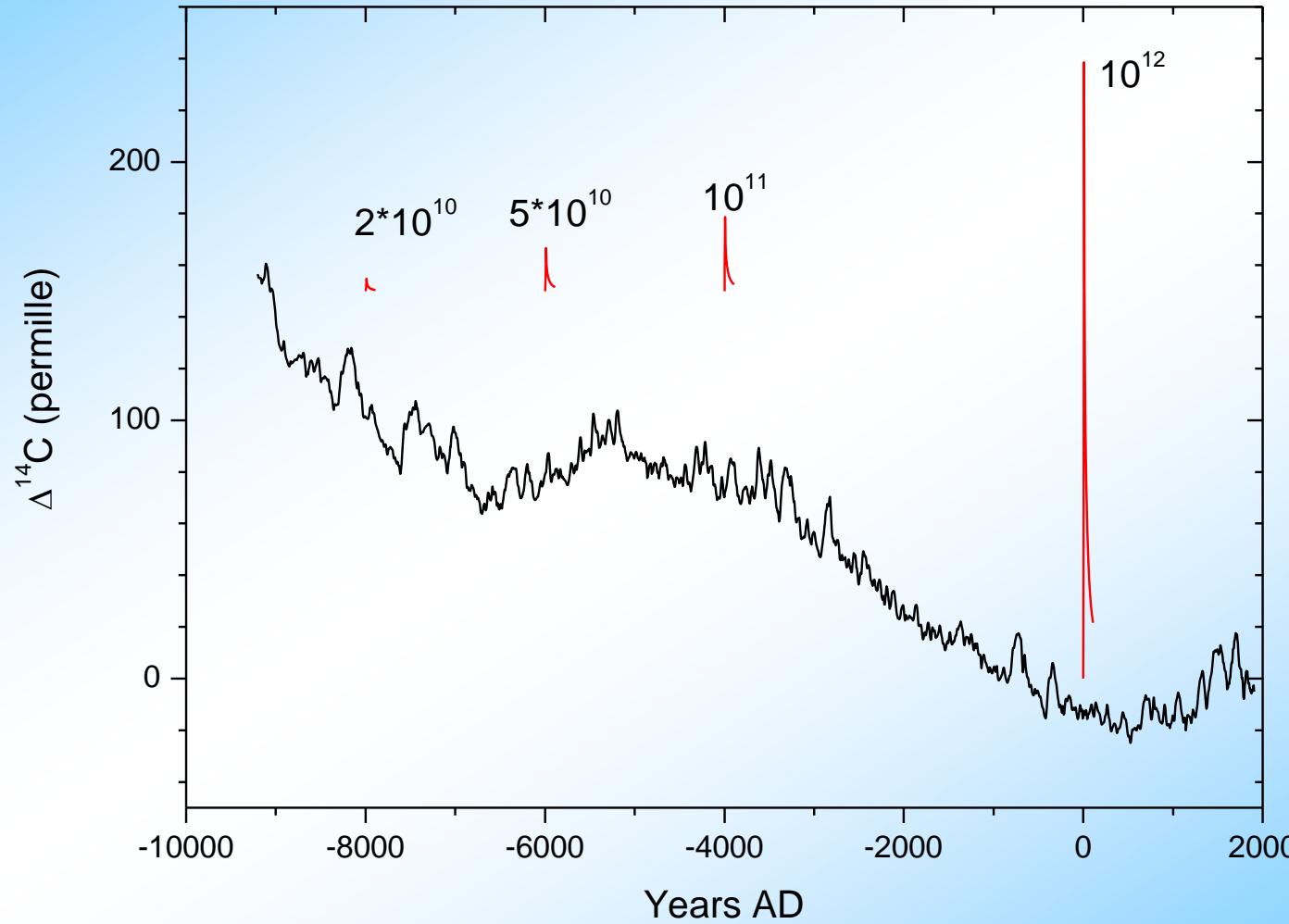
assumption was made that all of that nuclide was made by one huge SPE at one half-life of that radionuclide ago. These four limits define a line that drops



Inconsistency:

an event in ^{14}C (6 kyr) must leave record in ^{41}Ca (~ 100 kyr), etc.

Events to look for in $\Delta^{14}\text{C}$



Some formalism

$$\langle F \rangle = \int_0^{F_0} F \cdot p(F) \cdot dF + \int_{F_0}^{\infty} F \cdot p(F) \cdot dF = \langle F_1 \rangle + \langle F_2 \rangle,$$

Low-fluence events

High-fluence events

For 1955-2007, $\langle F \rangle = 1.1 \times 10^9 \text{ /cm}^2\text{/yr}$

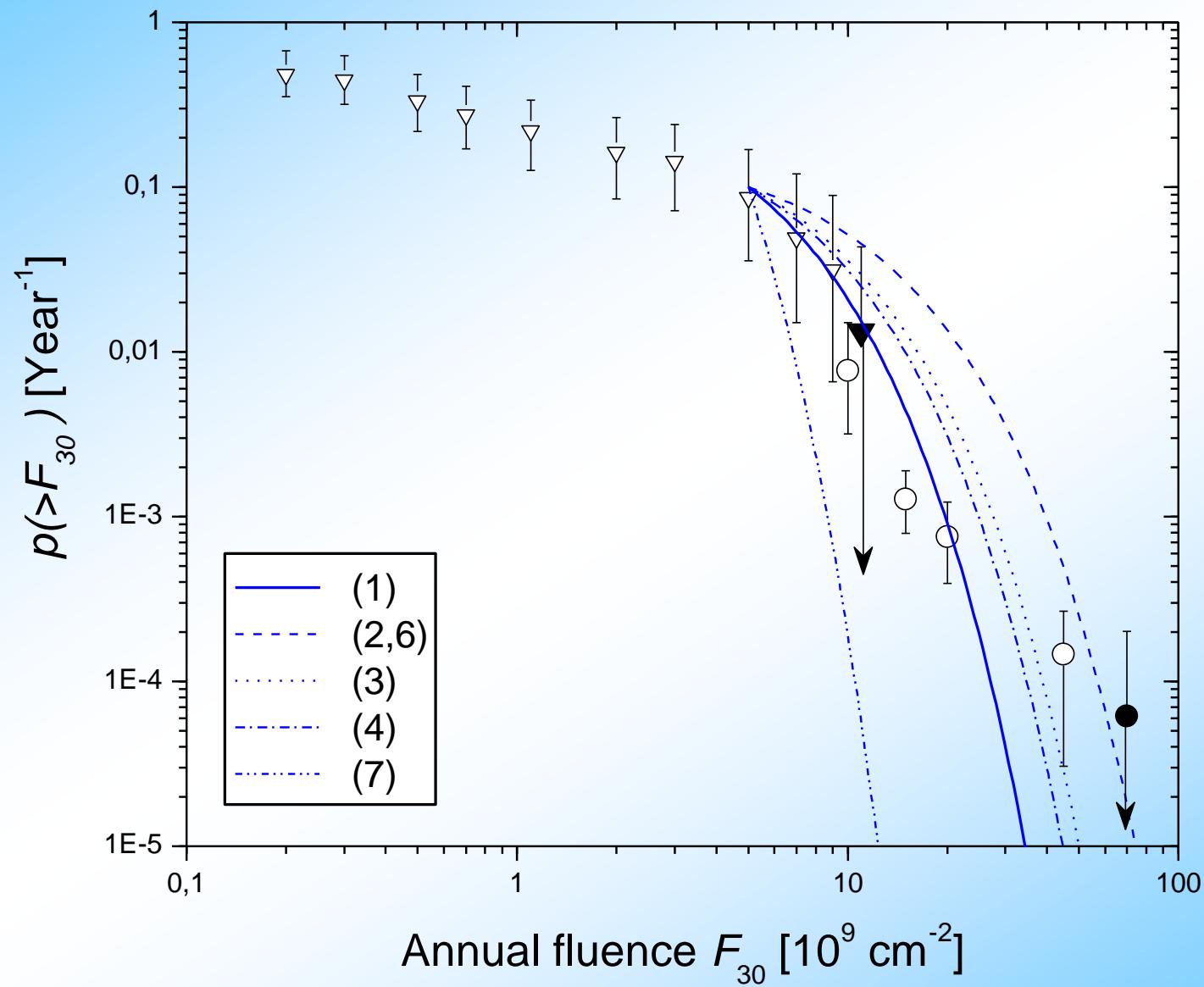
$P_o = 0.1 \text{ yr}^{-1}$, $F_o = 0.52 \times 10^9 \text{ /cm}^2\text{/yr}$ ~1/2 $\langle F \rangle$

$$p = dP/dF$$

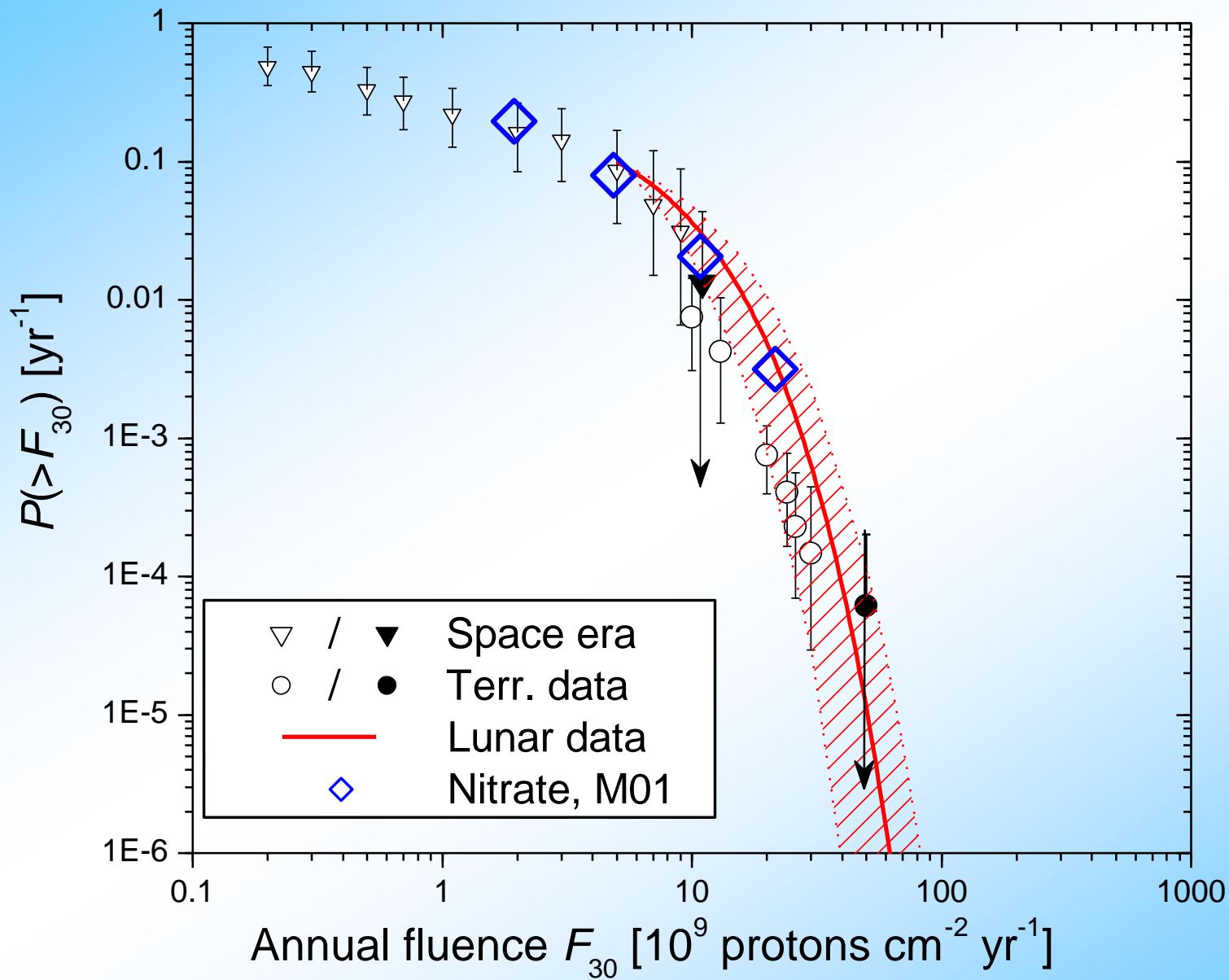
$P = P_o * (F/F_o)^{-\alpha} \rightarrow \text{power law}$

$P = P_o * \exp(\beta(F_o - F)) \rightarrow \text{exponential}$

Exponential OPDF



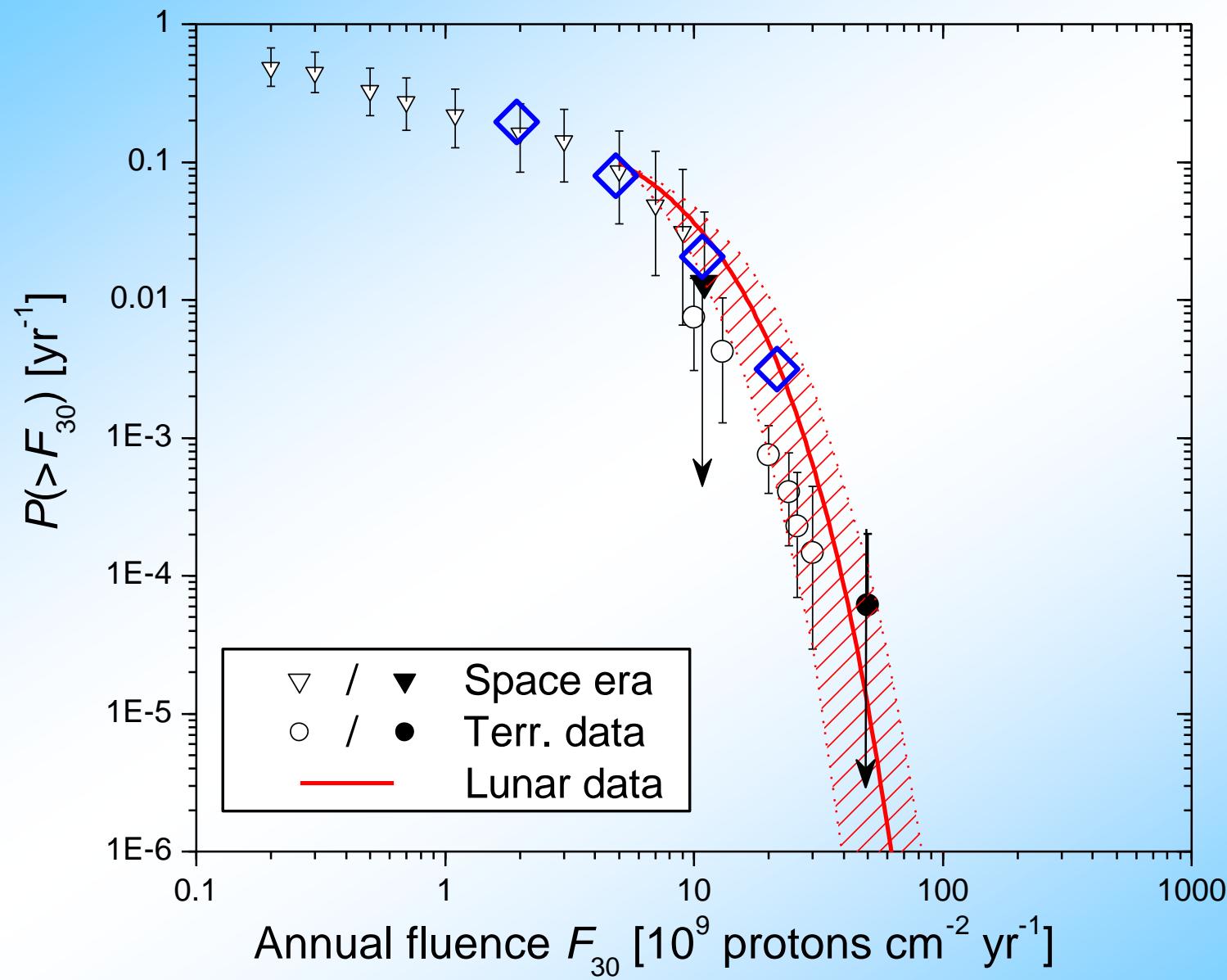
Final result



Summary on lunar rock-based SEP assessments

- Earlier estimates based on unrealistic assumptions (all F_{30} caused by a single event occurred at half-life time ago) → too high fluxes.
- A more realistic assumption → consistent with other independent data (terrestrial cosmogenic isotopes and "direct" observations).
- A strong roll-off is proposed for $F_{30} > 10^9$ protons/cm²/yr on average.
- The OP of a $F_{30} > 10^{11}$ p/cm²/yr event is $< 10^{-6}$ yr⁻¹.

Final result



THANK YOU !

SPE in ^{14}C

SEP → production → $Q_{^{14}\text{C}}$

(Kovaltsov et al., 2012)

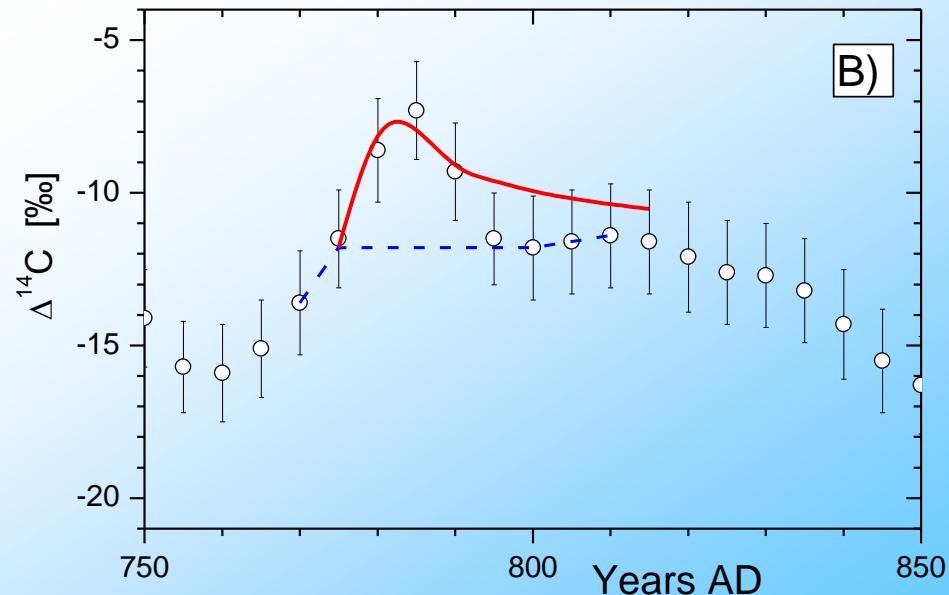
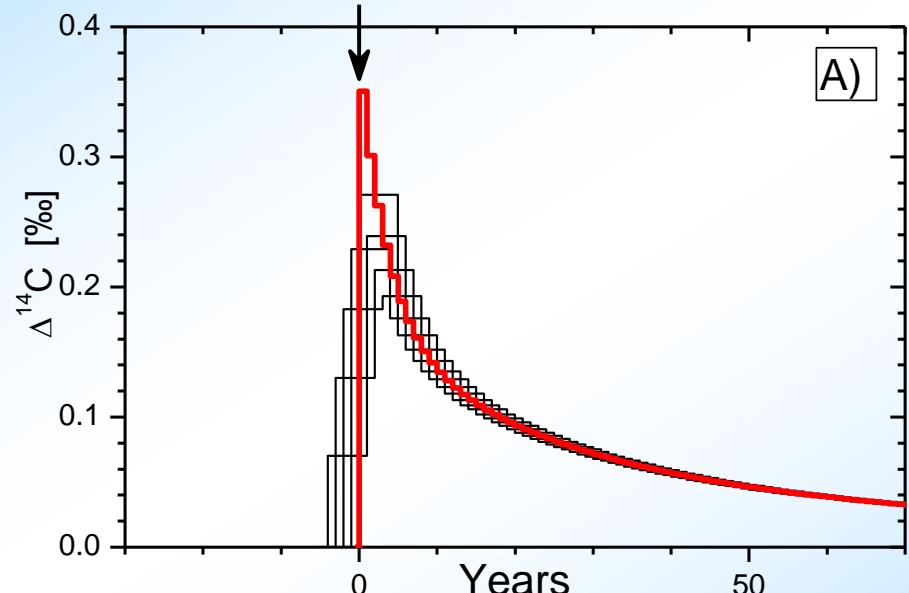
$Q \rightarrow$ carbon cycle $\rightarrow \Delta^{14}\text{C}$

5-box model (Damon & Peristykh, 2004)

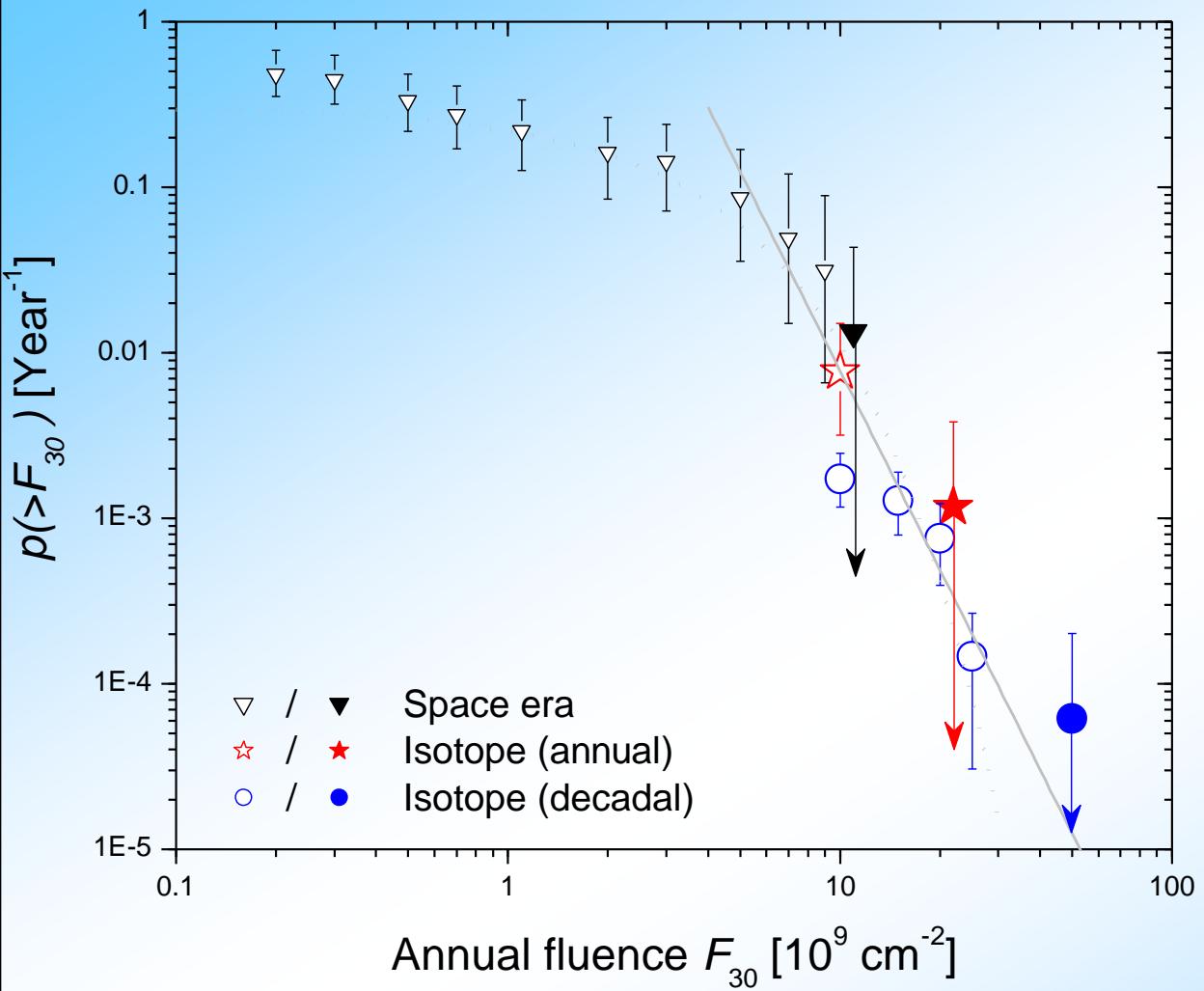
Response for SPE56 is:

Peak – 0.2-0.35 ‰ (errors ~2 ‰),
FWHM~20-30 yrs, rise time 0-10 yrs.

Fit of 24 SPE56 ($F_{30}=2.4 \times 10^{10} \text{ cm}^{-2}$) →



Lunar rocks



$$f'_{30} \sim 35 \text{ cm}^{-2} \text{ s}^{-1} \text{ for Space era}$$

(Shea & Smart, 2002; Reedy, 2012)

Fitting tail $> 7 \times 10^9 \text{ cm}^{-2}$:

$$\sim \exp(-0.33 \times 10^{-9} F_{30}) \text{ or } \sim F_{30}^{-4}$$

$$f''_{30} \sim 3.2-3.5 \text{ cm}^{-2} \text{ s}^{-1} \text{ for extreme SPEs}$$



$$f_{30} = f' + f'' = 38-39 \text{ cm}^{-2} \text{ s}^{-1}$$

Lunar rocks:

$$F_{30} = 21-56 (\sim 40) \text{ cm}^{-2} \text{ s}^{-1}$$

Totally consistent

SPE72 scenario:

$$f''_{30} \sim 110-130 \text{ cm}^{-2} \text{ s}^{-1} \rightarrow$$

$$f_{30} \sim 150 \text{ cm}^{-2} \text{ s}^{-1} - \text{*inconsistent*}$$

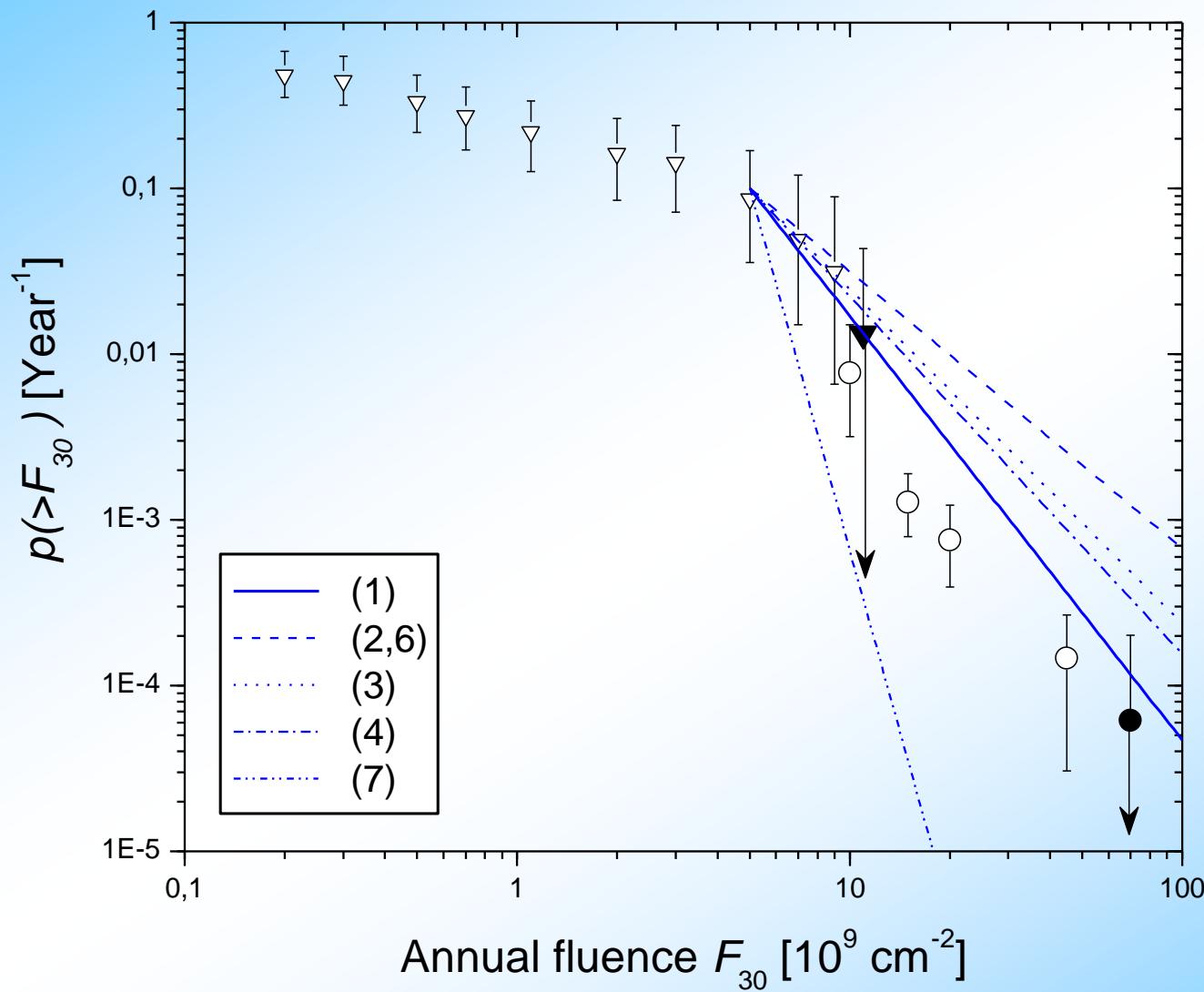
Extreme SPEs should have hard spectra!

Lunar rock data

Table 1. Assessments of the parameters of OPDF from different cosmogenic radionuclide data in lunar rocks. Columns correspond to the nuclide, reference to the original data, the measured mean annual fluence F^* (10^9 protons/cm 2 /yr), and the corresponding best-fit parameters α and β (10^{-9} cm 2 yr) with the 90% confidence intervals (see text).

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| 5 | ^{26}Al | (Kohl <i>et al.</i> , 1978) | 0.79 | N/A | N/A |
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| 11 | ^{53}Mn | (Kohl <i>et al.</i> , 1978) | 0.79 | N/A | N/A |

Power-law OPDF



Some formalism

$$\langle F \rangle = \int_0^{F_0} F \cdot p(F) \cdot dF + \int_{F_0}^{\infty} F \cdot p(F) \cdot dF = \langle F_1 \rangle + \langle F_2 \rangle,$$

For 1955-2007, $\langle F \rangle = 1.1 \times 10^9 \text{ /cm}^2\text{/yr}$

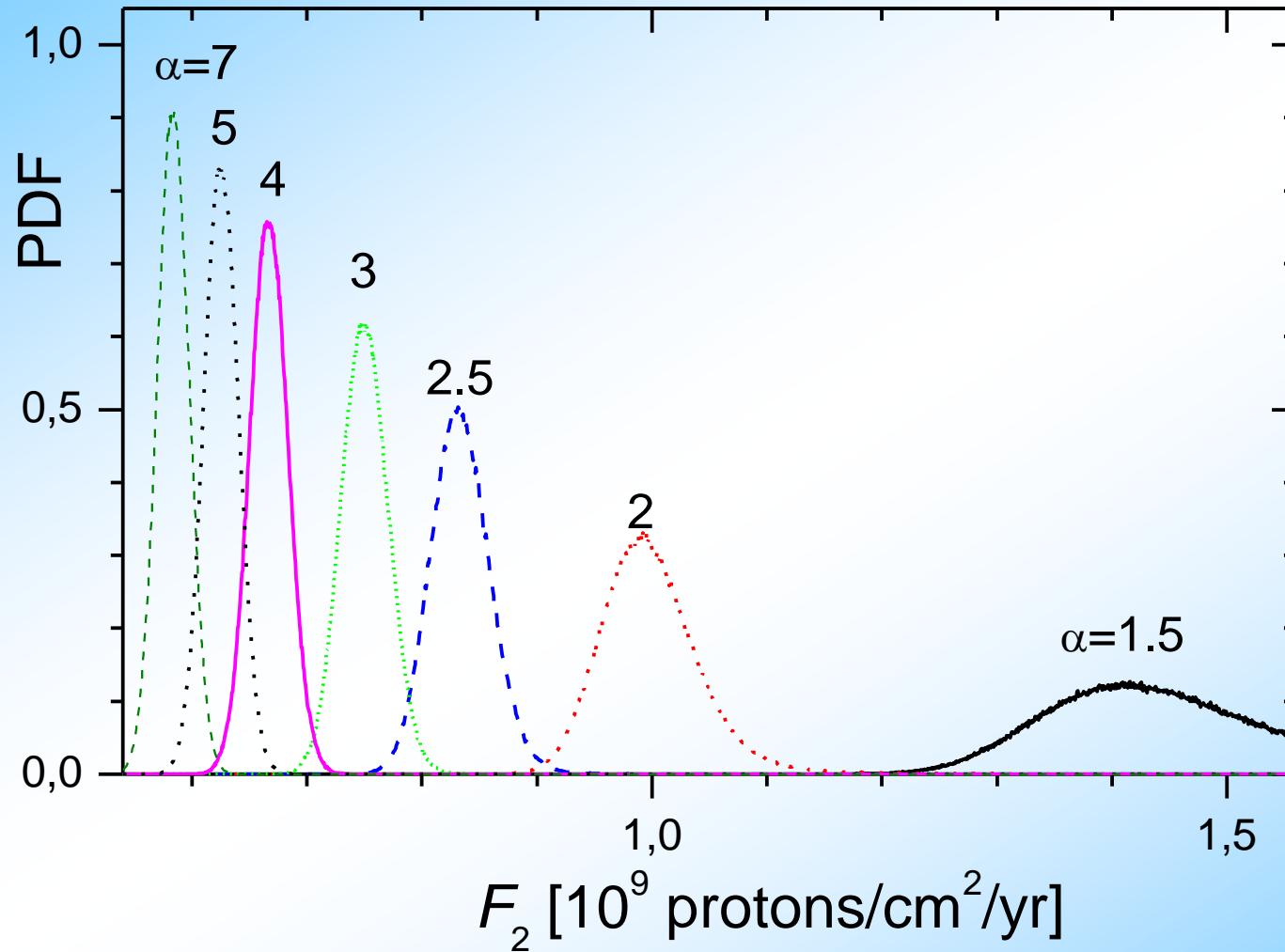
$$P_o = 0.1 \text{ yr}^{-1}, F_o = 0.52 \times 10^9 \text{ /cm}^2\text{/yr}$$

$$p = dP/dF$$

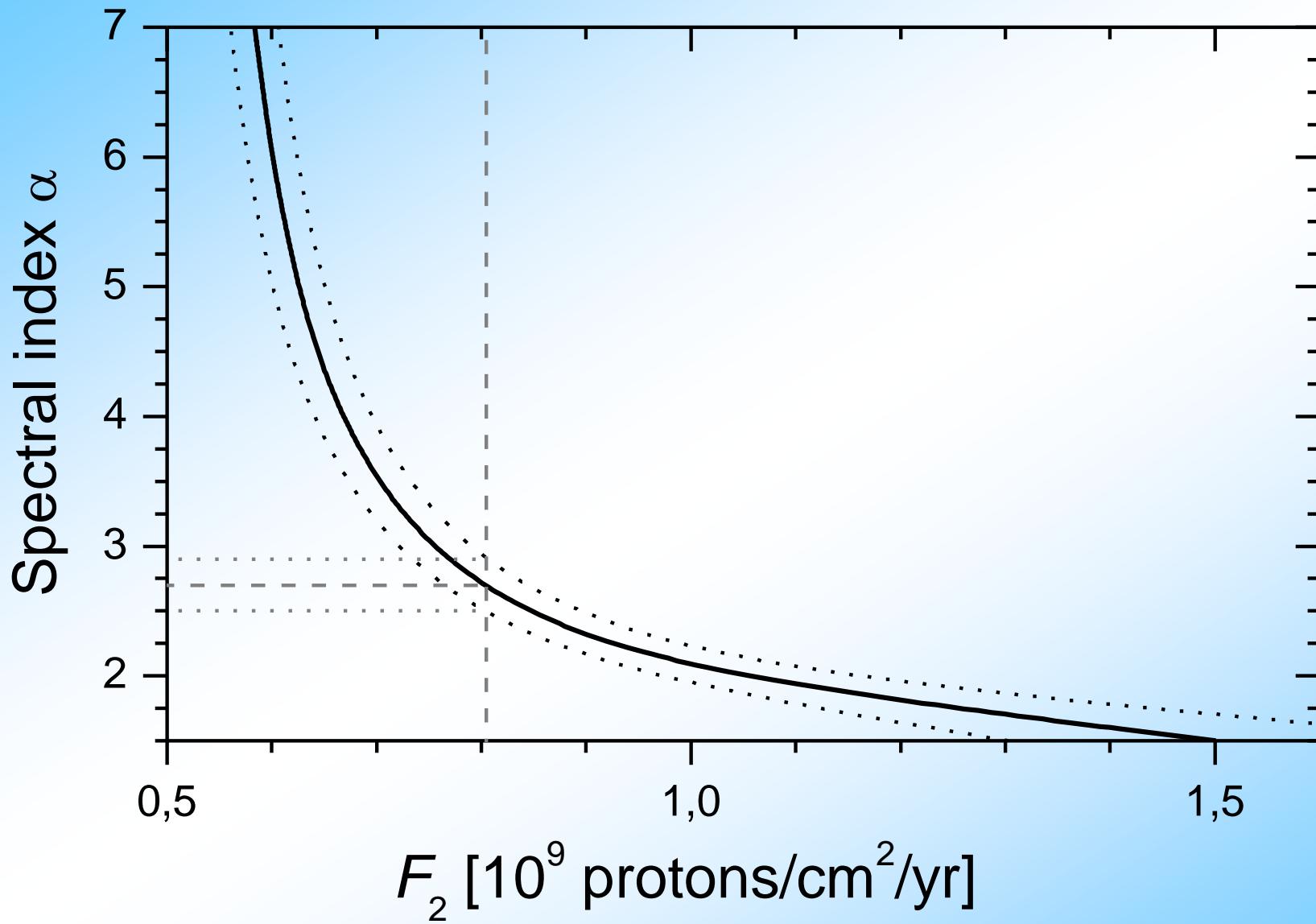
$$P = P_o * (F/F_o)^{-\alpha} \rightarrow \text{power law}$$

$$P = P_o * \exp(\beta(F_o - F)) \rightarrow \text{exponential}$$

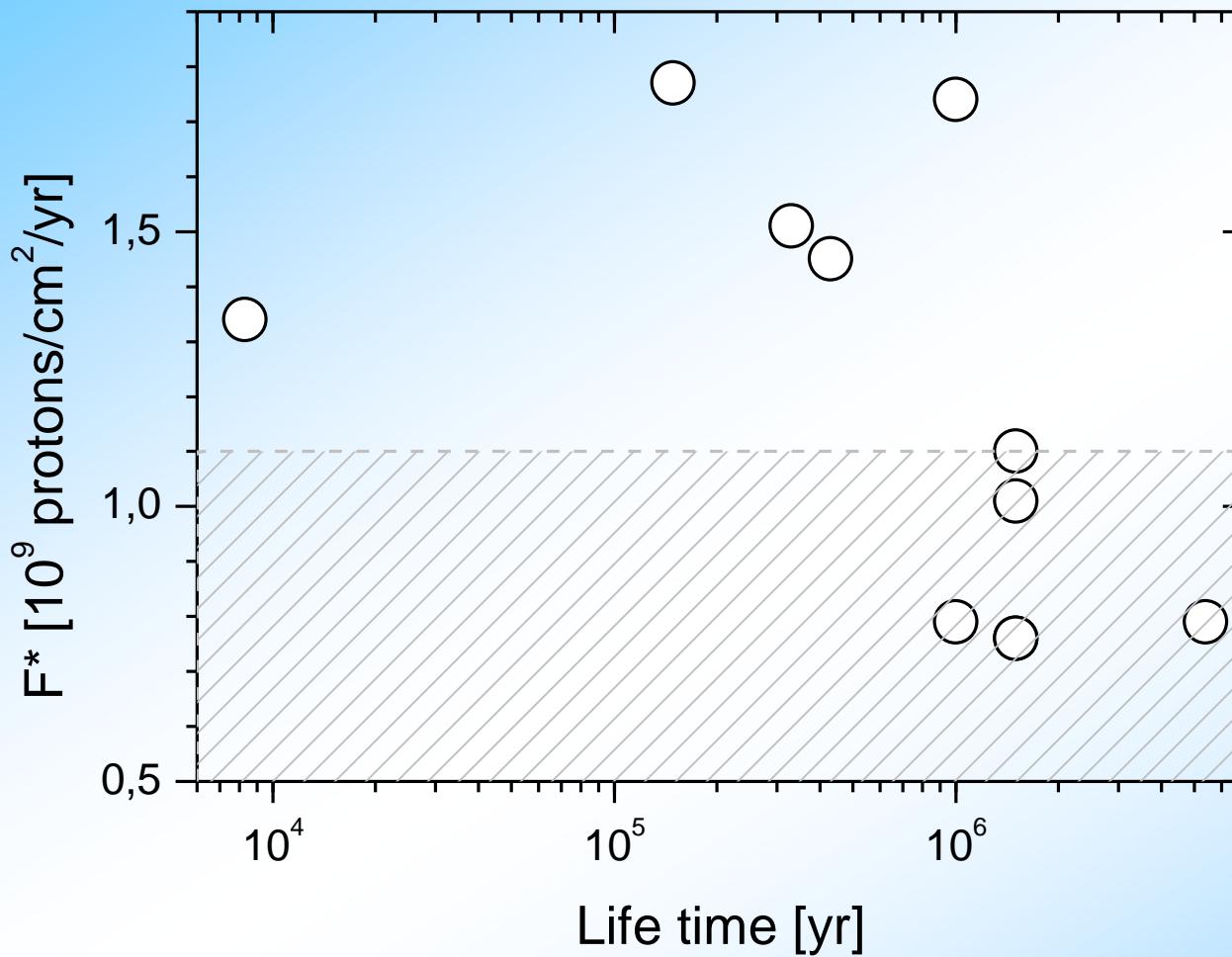
PDF vs. F2



Calibration curve



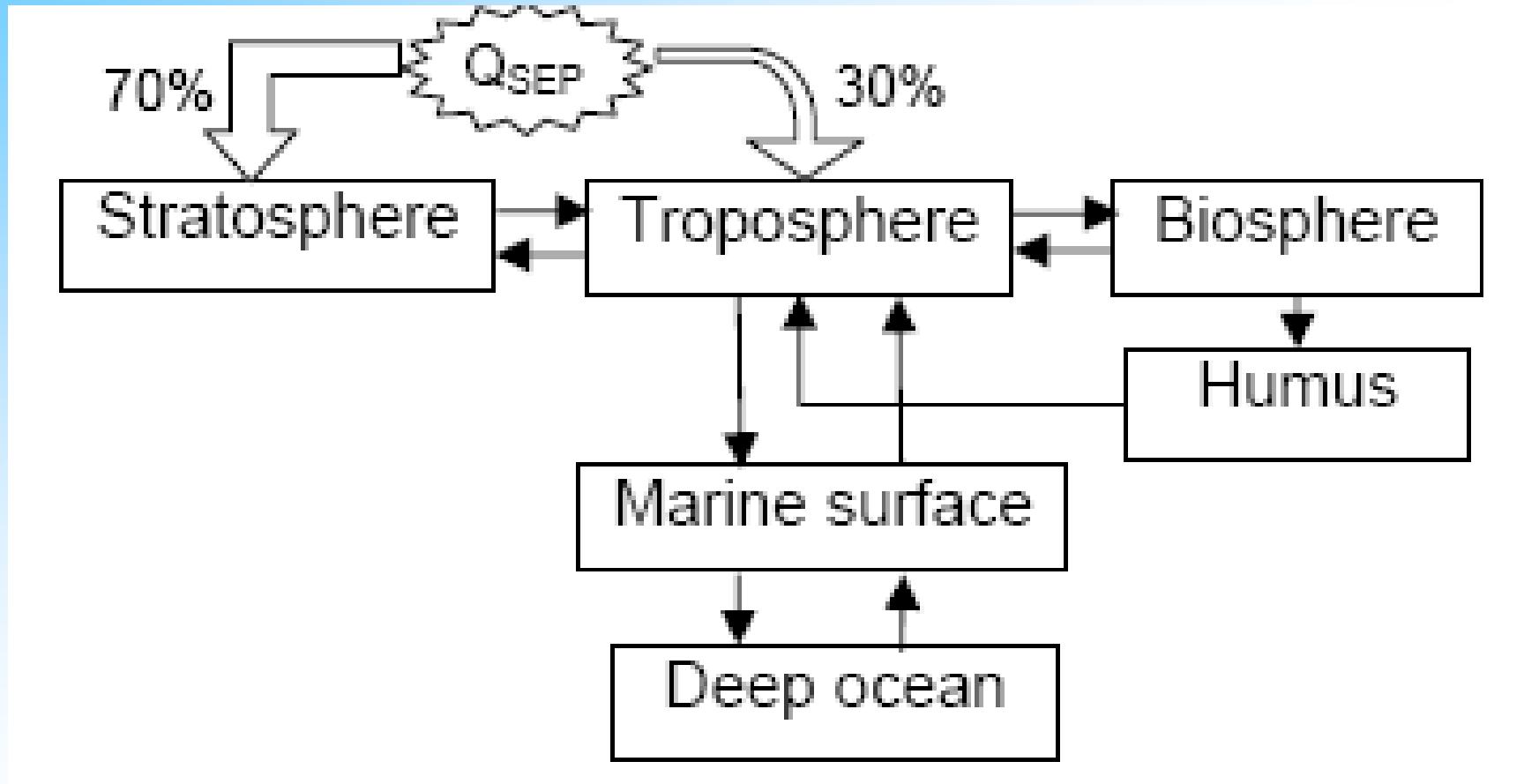
Lunar rock data



Such a situation is impossible!

Even switching SEP off does not help → neglect long-living isotopes.

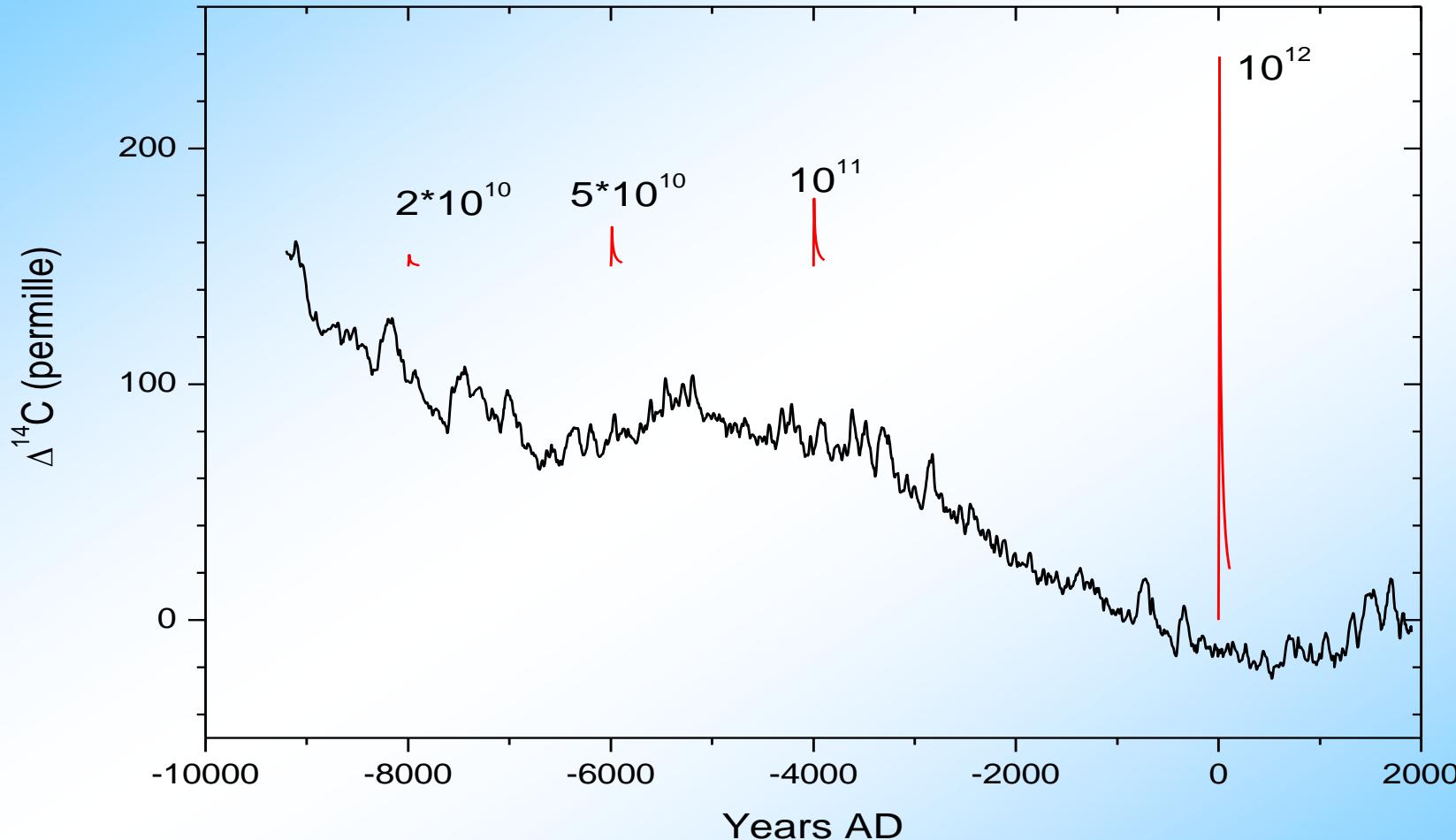
Scheme



Lunar rock vs. $\Delta^{14}\text{C}$

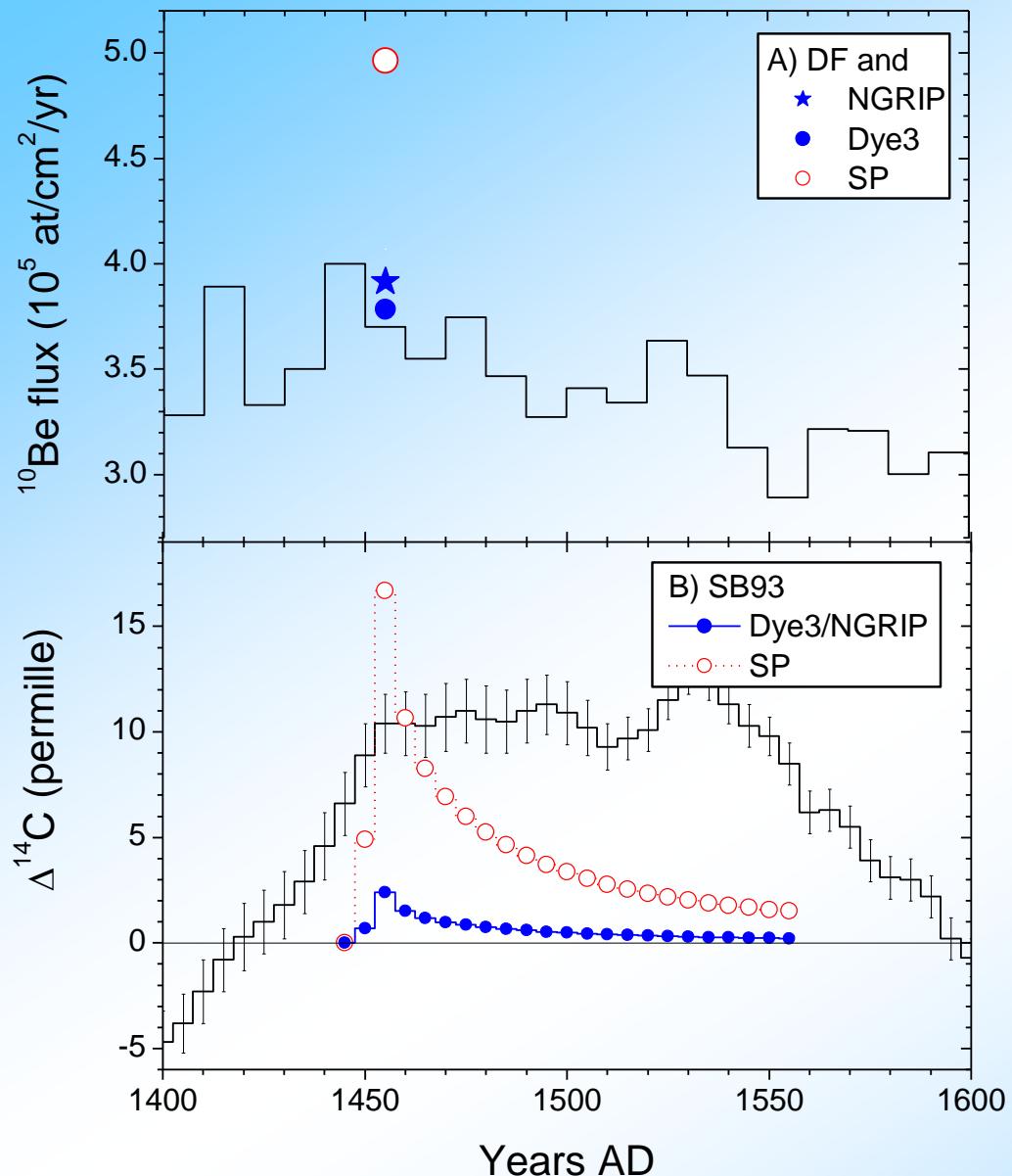
Lunar rock-based limit: Half of the fluence – by one SPE **BUT**:

$^{14}\text{C-LR}$ based estimate $f \sim 42 \text{ cm}^{-2}\text{s}^{-1}$ (Jull et al.), for non-extreme SPEs $f \sim 35 \text{ cm}^{-2}\text{s}^{-1} \Rightarrow$ for extreme SPE $f \sim 7 \text{ cm}^{-2}\text{s}^{-1} \Rightarrow$ total F_{30} fluence $\sim 2 \cdot 10^{12} \text{ cm}^{-2}$ over Holocene \Rightarrow max $\sim 10^{12} \text{ cm}^{-2}$.



Lunar rocks: A few $F_{30}=10^{13}$ events over Holocene – must be seen in $\Delta^{14}\text{C}$ series.

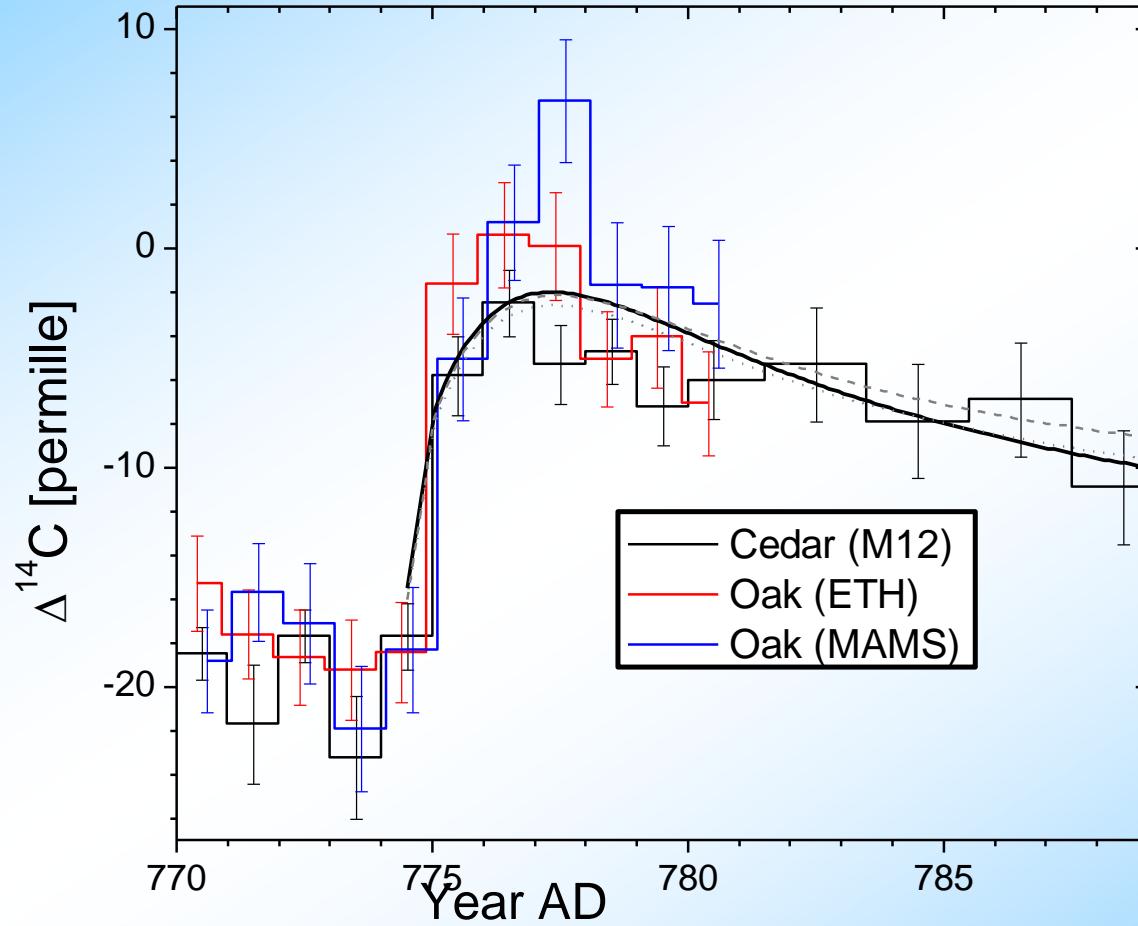
Specific event of ca. 1460 AD



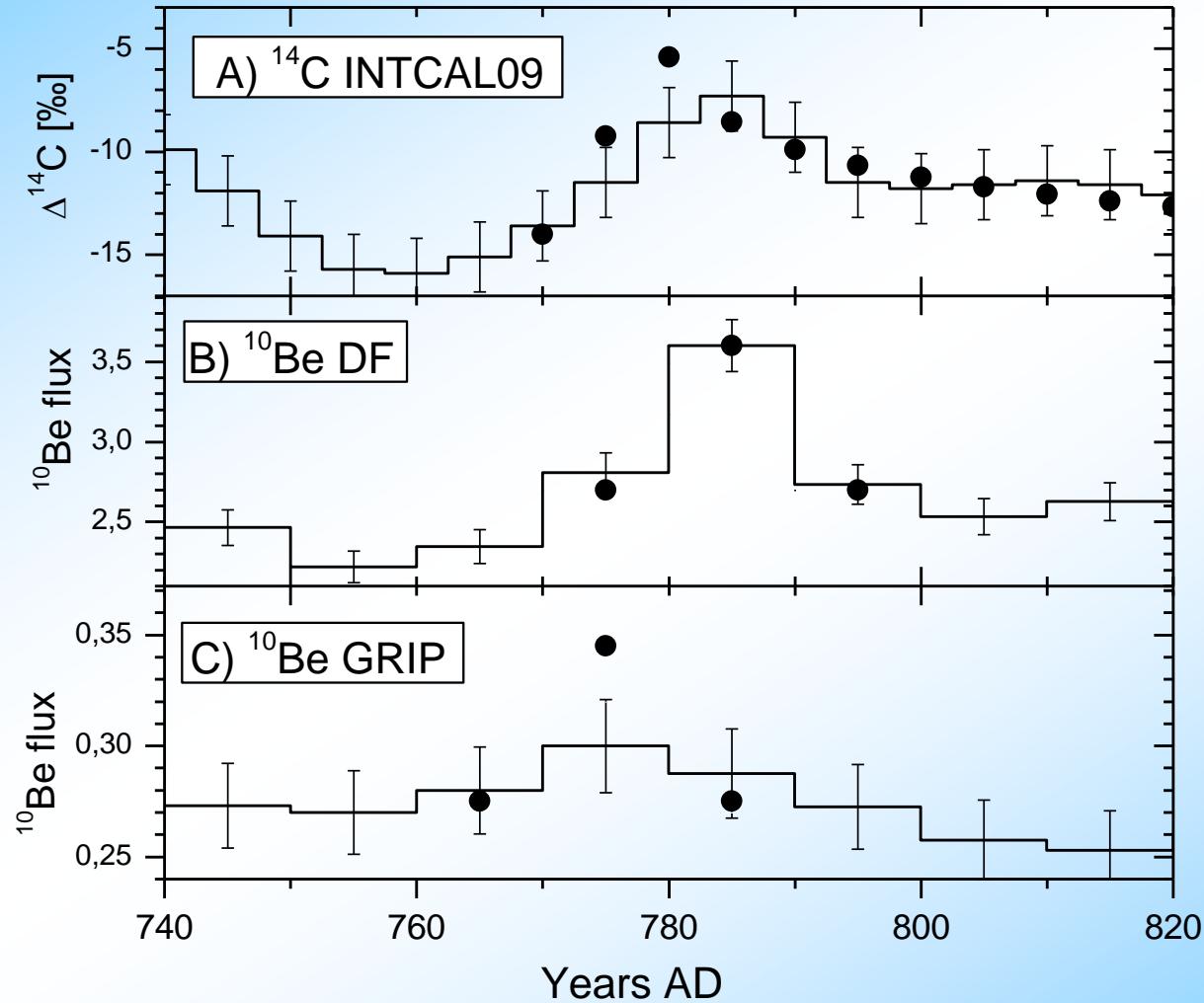
NGRIP/Dye3 signal ($F_{30}=(1-1.5)*10^{10} \text{ cm}^{-2}$) is consistent with DF and SB93 (no signal),

SP-implied signal ($F_{30}=7*10^{10} \text{ cm}^{-2}$) – too high

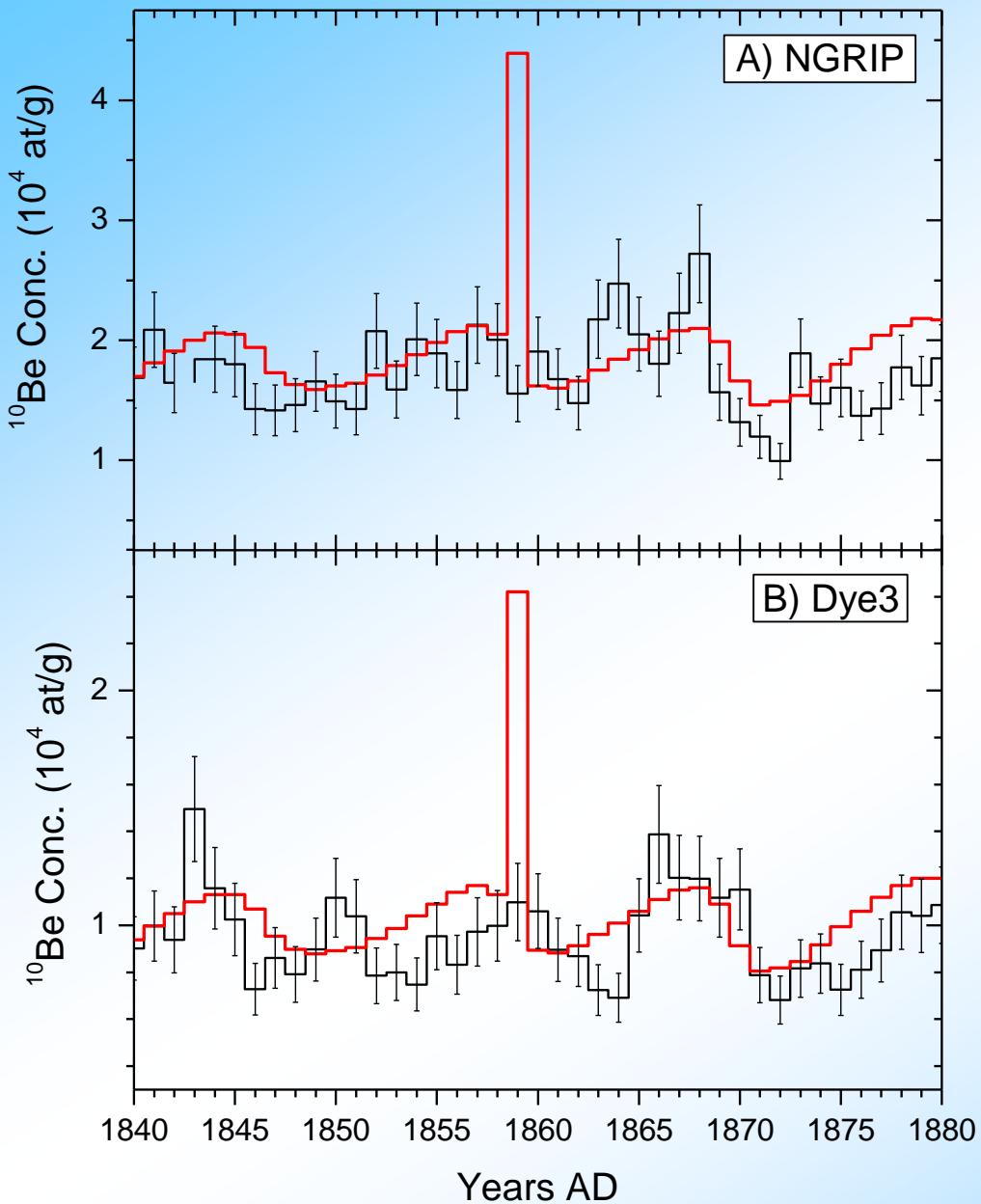
775 AD: model vs. data



780 AD – other data



Carrington event 1859



Carrington event 1859:

$F_{30} = 1.8 \times 10^{10} \text{ cm}^{-2}$ (McCracken et al., 2001).

+

GCR (from Alanko-Huotari et al., 2007)

+

^{10}Be production model (Kovaltsov & Usoskin, 2010)

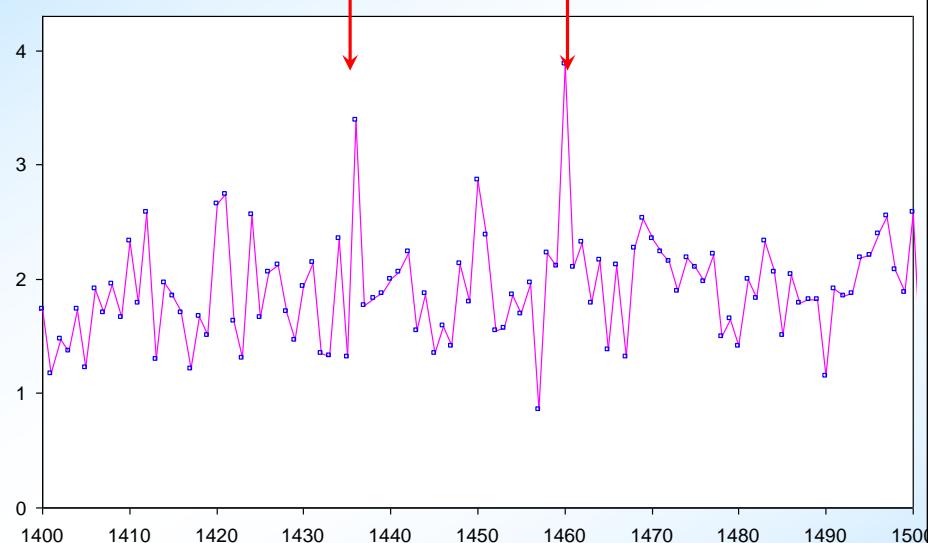
→

modelled ^{10}Be response.

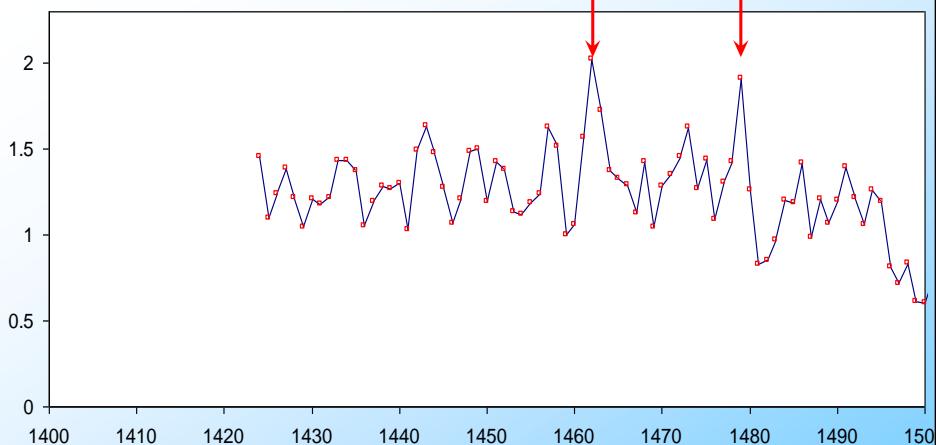
The expected peak is $\sim 10 \sigma$ too high =>
Should be $< 5 \times 10^9 \text{ cm}^{-2}$.

Potential signature in annual ^{10}Be

- **NGRIP** series: peaks $> 1.3 \times 10^4$ at/g
1436, 1460, 1650, 1719, 1810, 1816, 1965



- **Dye3** series: peaks $> 0.6 \times 10^4$ at/g
1462, 1479, 1505, 1512, 1603



- **SB93** series: no peaks identified

Cross-check performed

SPEs: all data

