

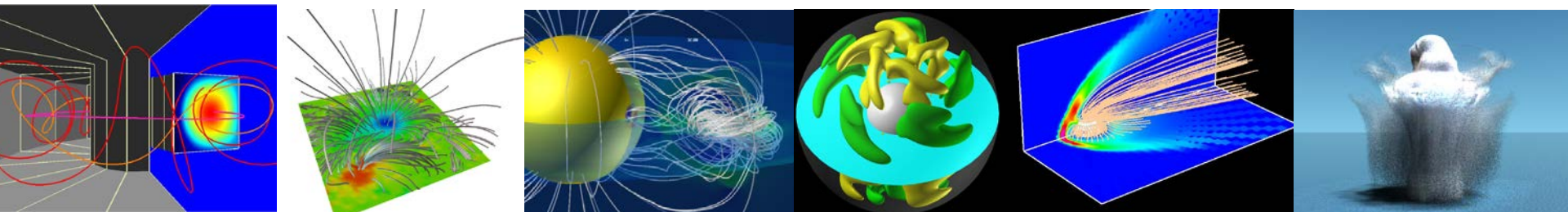
The banner features a large orange sun on the left with white magnetic field lines extending across the top. On the right, a small Earth is shown with a satellite orbiting it. The text is centered in white.

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# Hemispheric Asymmetry of Solar Cycle Activities

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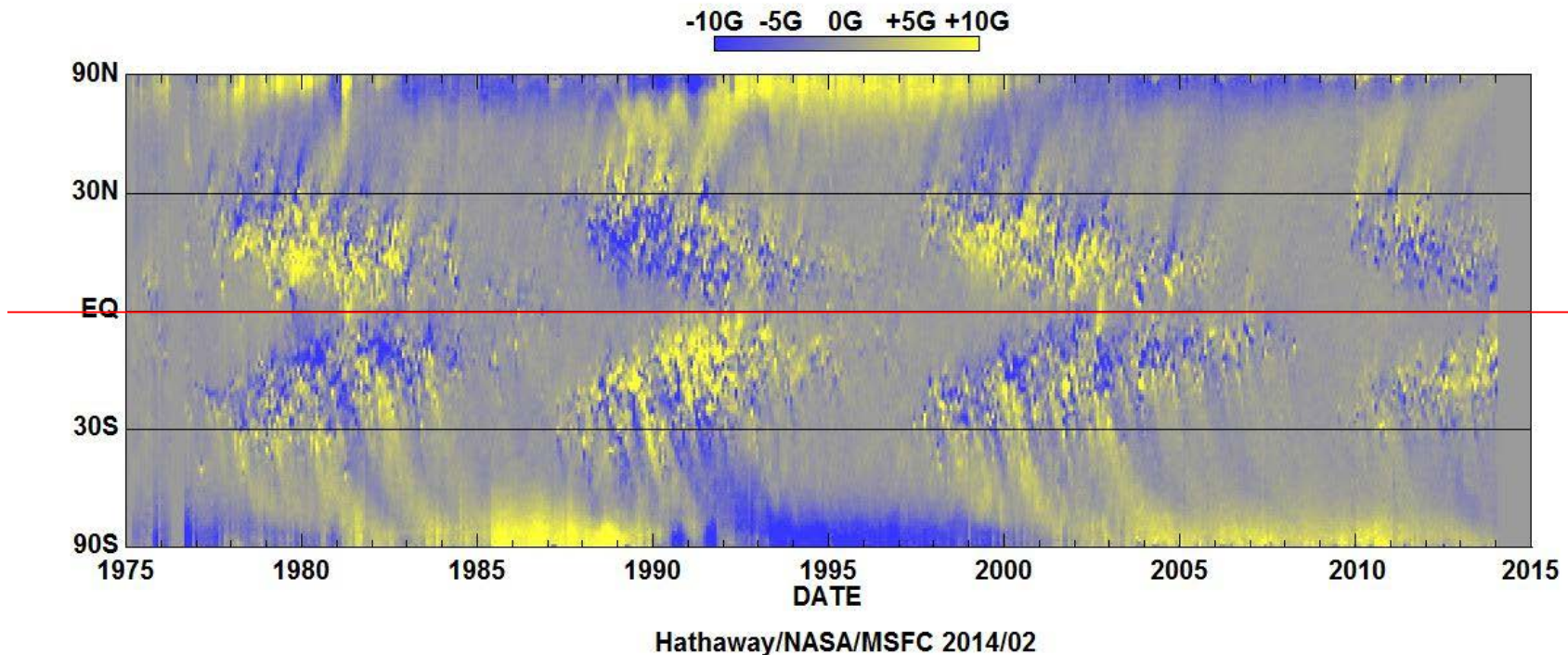
# Outlook

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- Introduction
  - What is the hemispheric asymmetry of solar cycle? Why should we study it?
  - Review of previous studies
    - Observations and Simulations
- **【Our study】** A simple dynamo model of hemispheric asymmetry
  - Numerical Model
  - Results
- Discussion and summary

# “Butterfly” is almost symmetric.

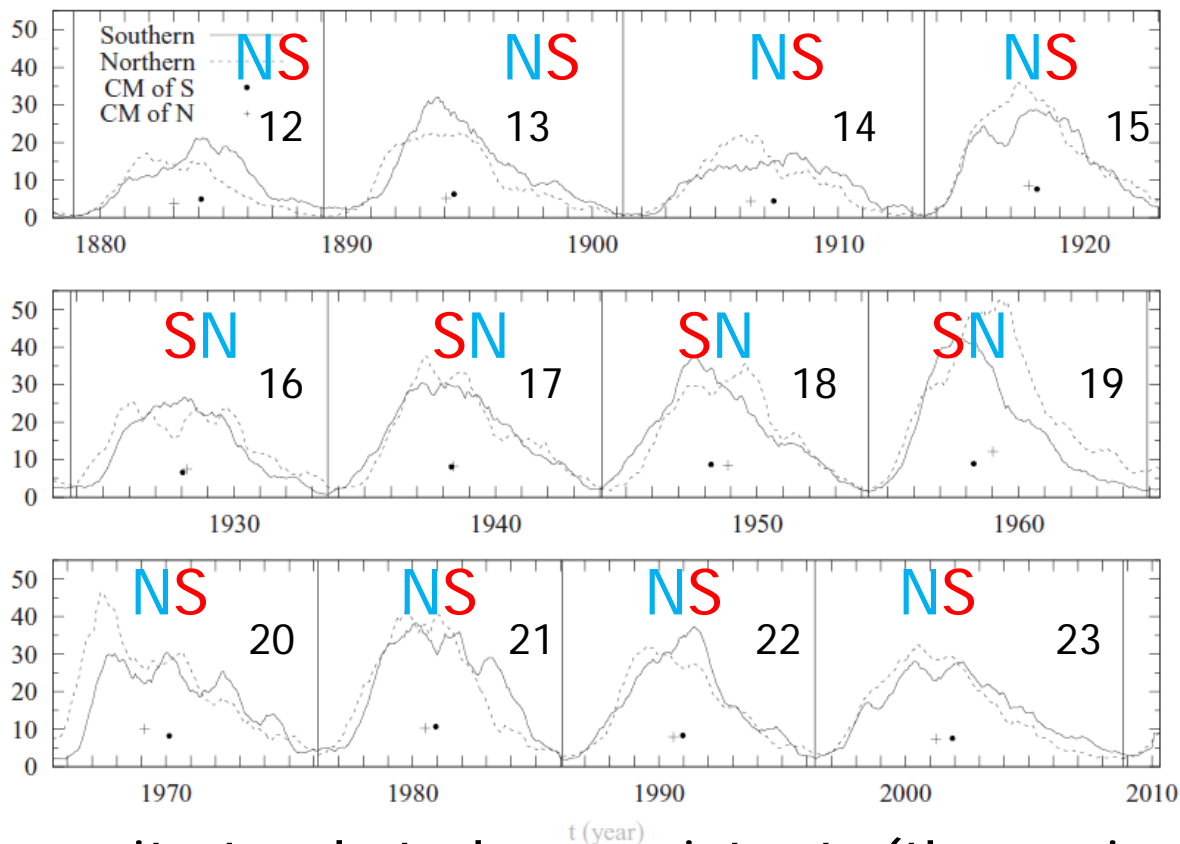
- Magnetic field on the solar surface



# Hemispheric Asymmetry

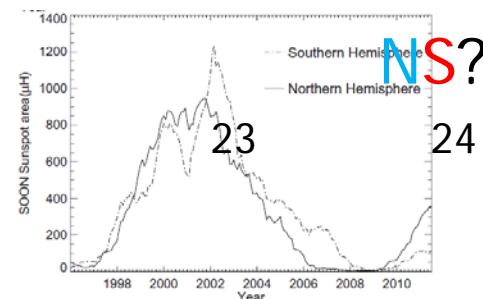
- Phase of solar (sunspot) cycles

hemispheric sunspot group number



Muraközy & Ludmány 2012

Ravindra & Javaraiah 2015



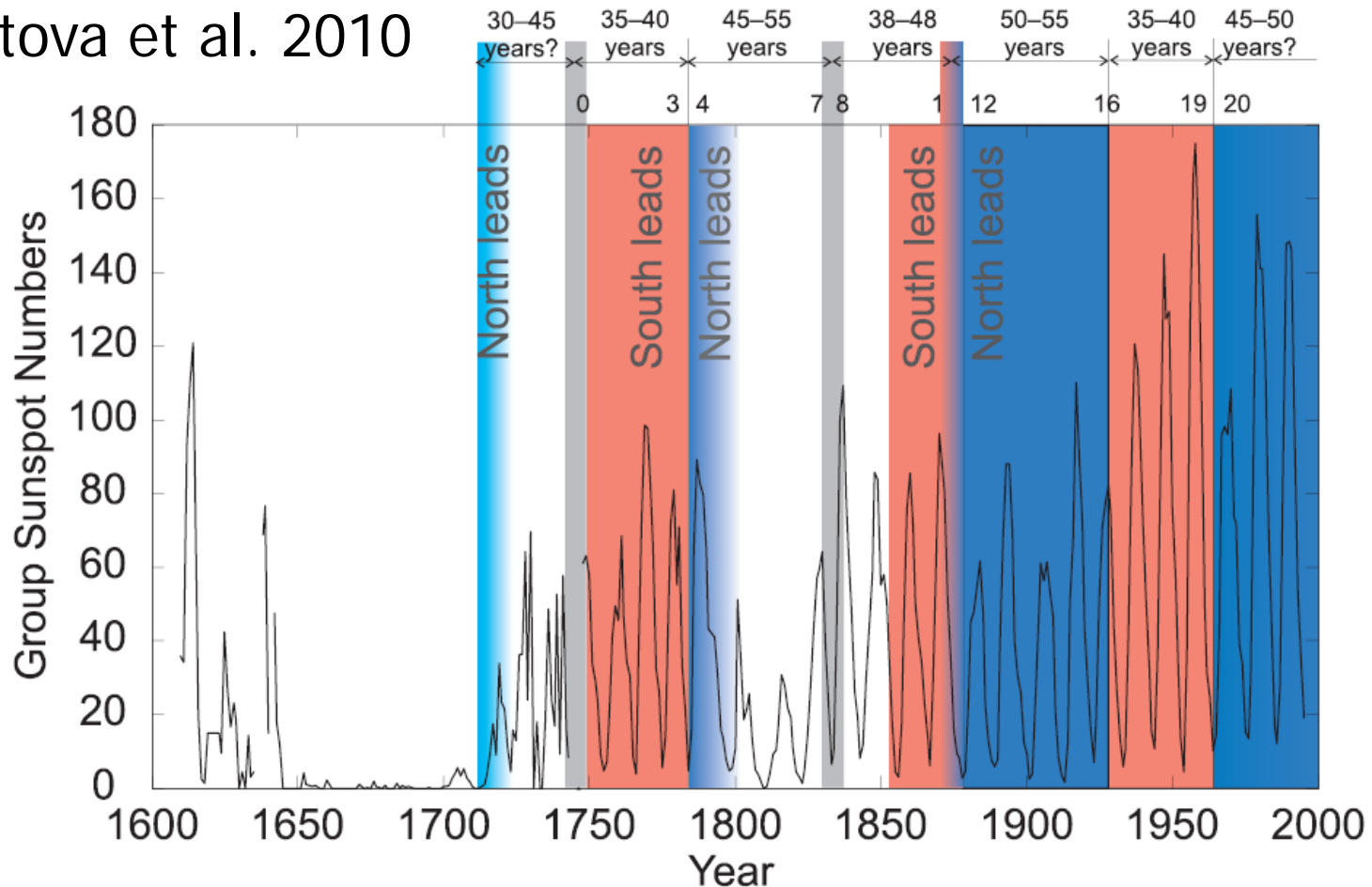
- The parity tends to be persistent. (the period of 4+4 cycle?)



# Long-term evolution of N-S symmetry

The north-south asymmetry exhibits a long-term persistence, and it should not be regarded as a stochastic phenomenon.

Zolotova et al. 2010



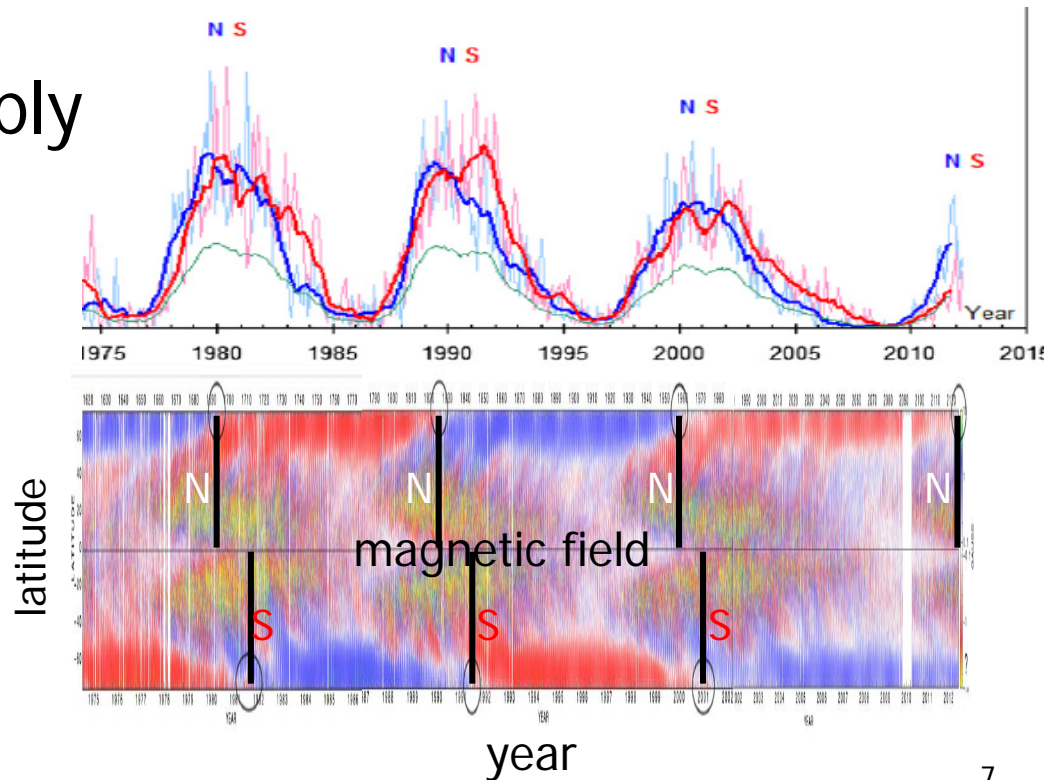
# Polar Field Reversal

- The polar field reversals have been at different times in the different hemispheres.

Babcock & Babcock 1955, Babcock 1959, Babcock 1961

- The asymmetric polar field reversals are simply a consequence of the asymmetry of sunspot activity.

Svalgaard & Kamide 2013



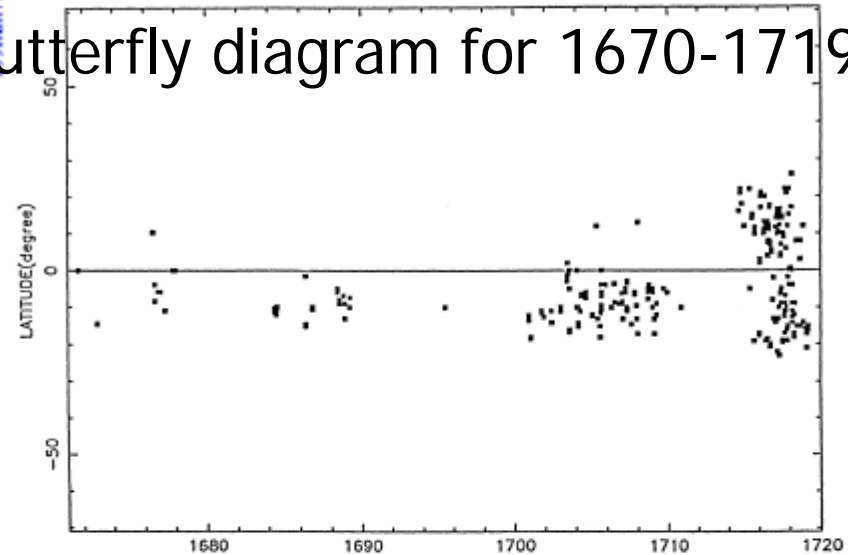
# Strong Asymmetry in Maunder Min.

Sokoloff and Nesme-Ribes (1994)

Strong asymmetry b/w north and south hemisphere might be observed during the Maunder minimum.

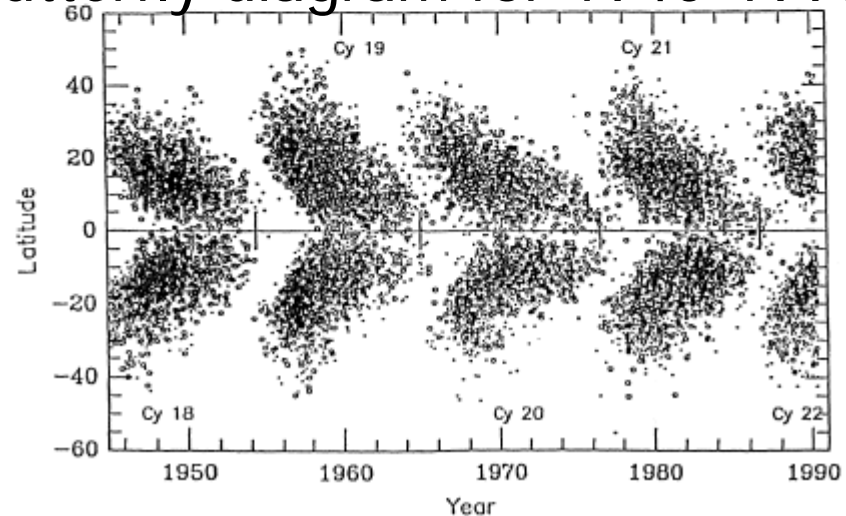
a BUTTERFLY DIAGRAM OF SUNSPOT, PARIS ARCHIVES : 1670-1719

Butterfly diagram for 1670-1719



b BUTTERFLY DIAGRAM OF SUNSPOT, PARIS ARCHIVES : 1940-1990

Butterfly diagram for 1940-1990



# Other Asymmetric Features

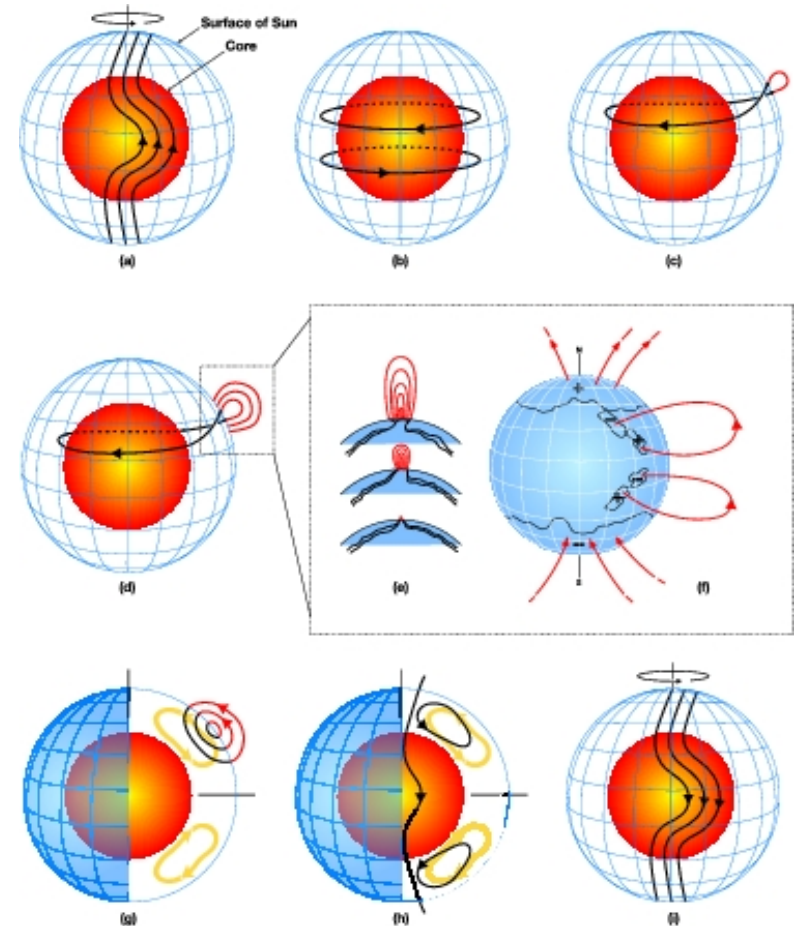
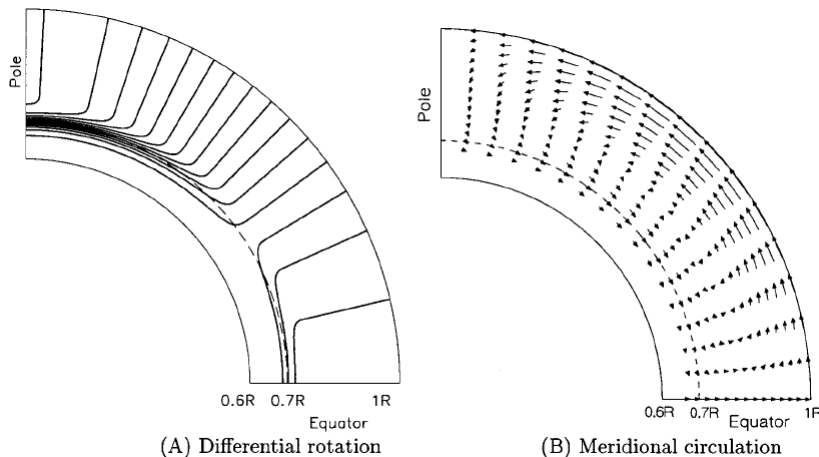
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- Mursula, Hiltula, Zieger 2002
  - Asymmetry of **solar wind** and **heliospheric current sheets** could be related to a persistent N-S asymmetry of solar dynamo.
- Feng, Deng, Xu 2013
  - Asymmetry of the **flare** index between the N-S hemispheres is about 6-7 months, which is near the time delay between flare activity and sunspot activity.
- Gopalswamy et al. 2012
  - Asymmetric behavior is revealed by **microwave observations**

# What is the cause of asymmetry?

## Dynamo

The most of flux transport dynamo models just assumed the hemispheric symmetry.



Dikpati & Charbonneau 1999  
Babcock-Leighton Flux Transport Dynamo

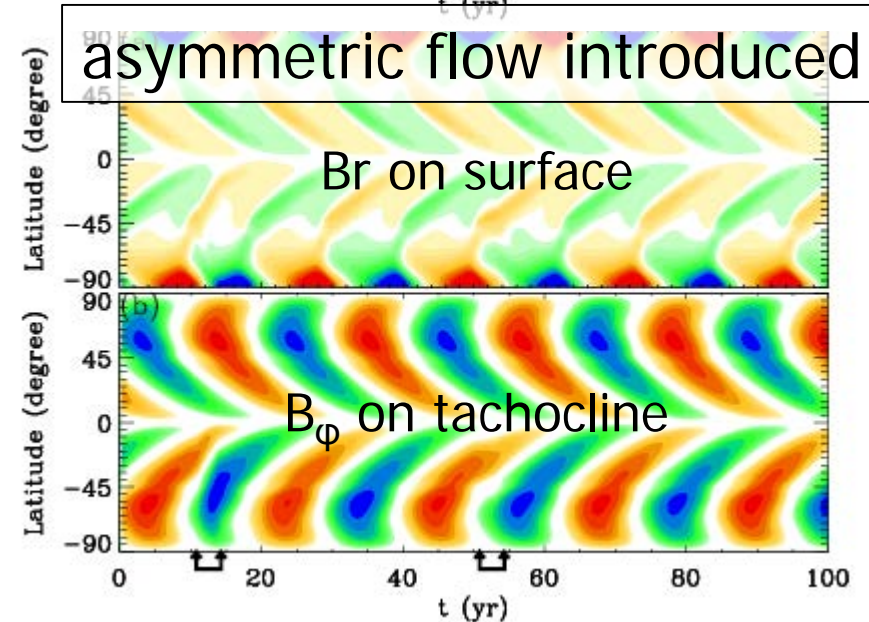
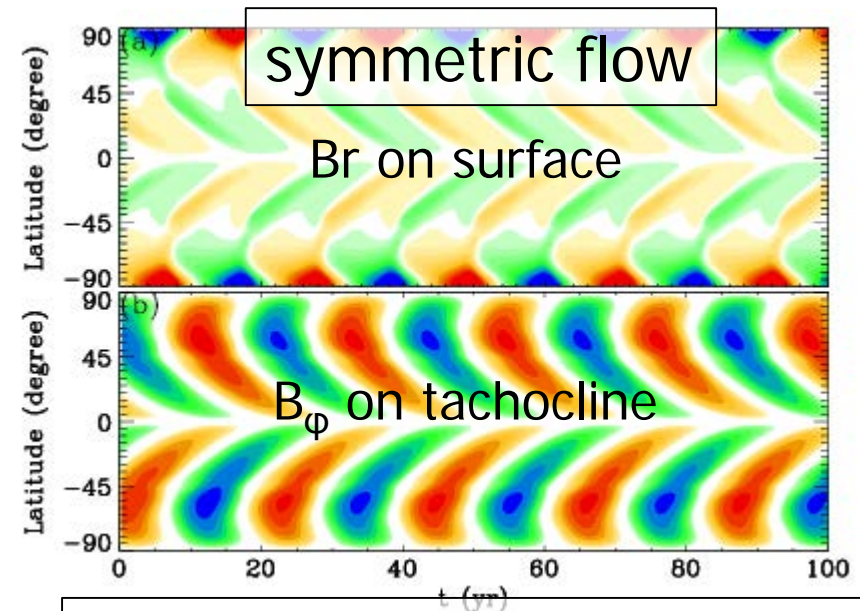
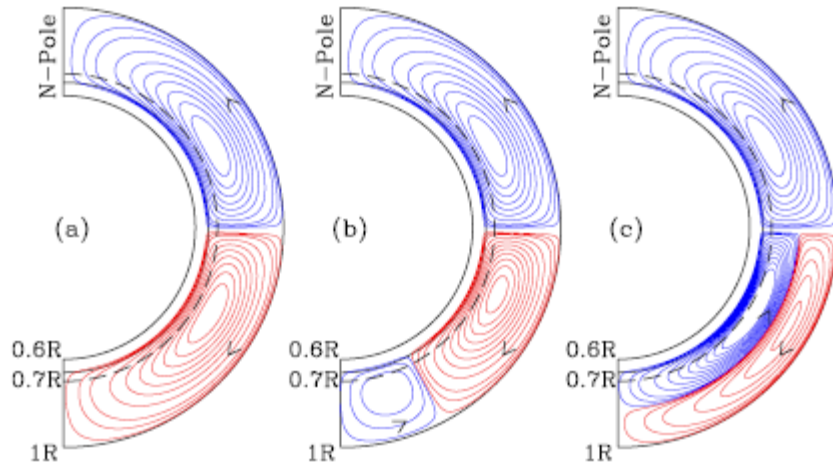


# Effects of Asymmetric Flow

## ■ Belucz & Dikpati 2013

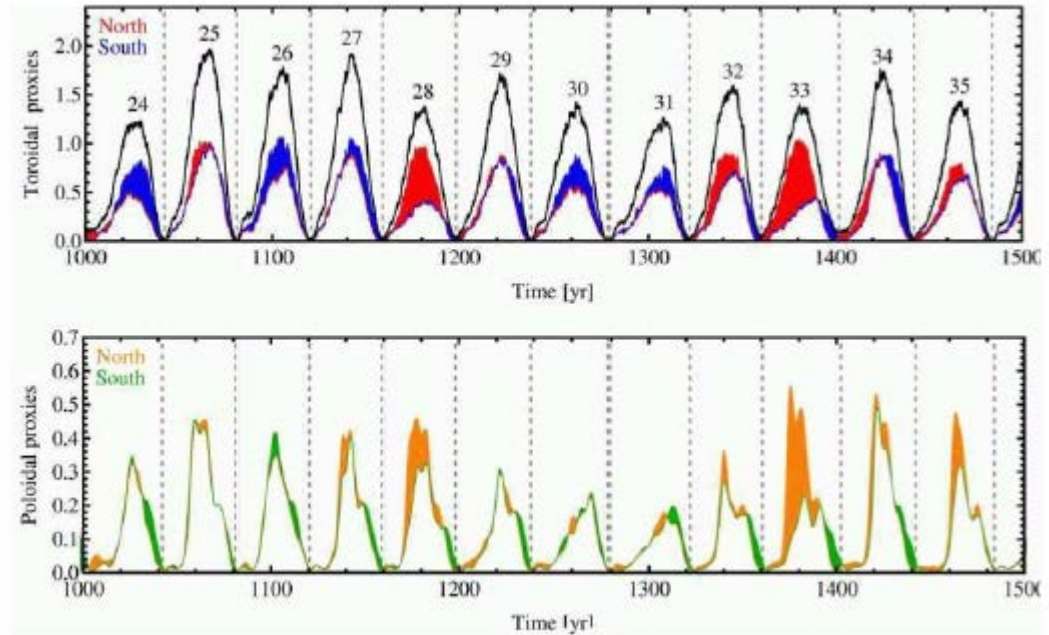
- Asymmetric meridional circulation
- 2D flux transport model

The asymmetry in meridional circulation produces differing cycles in the N-S hemispheres.



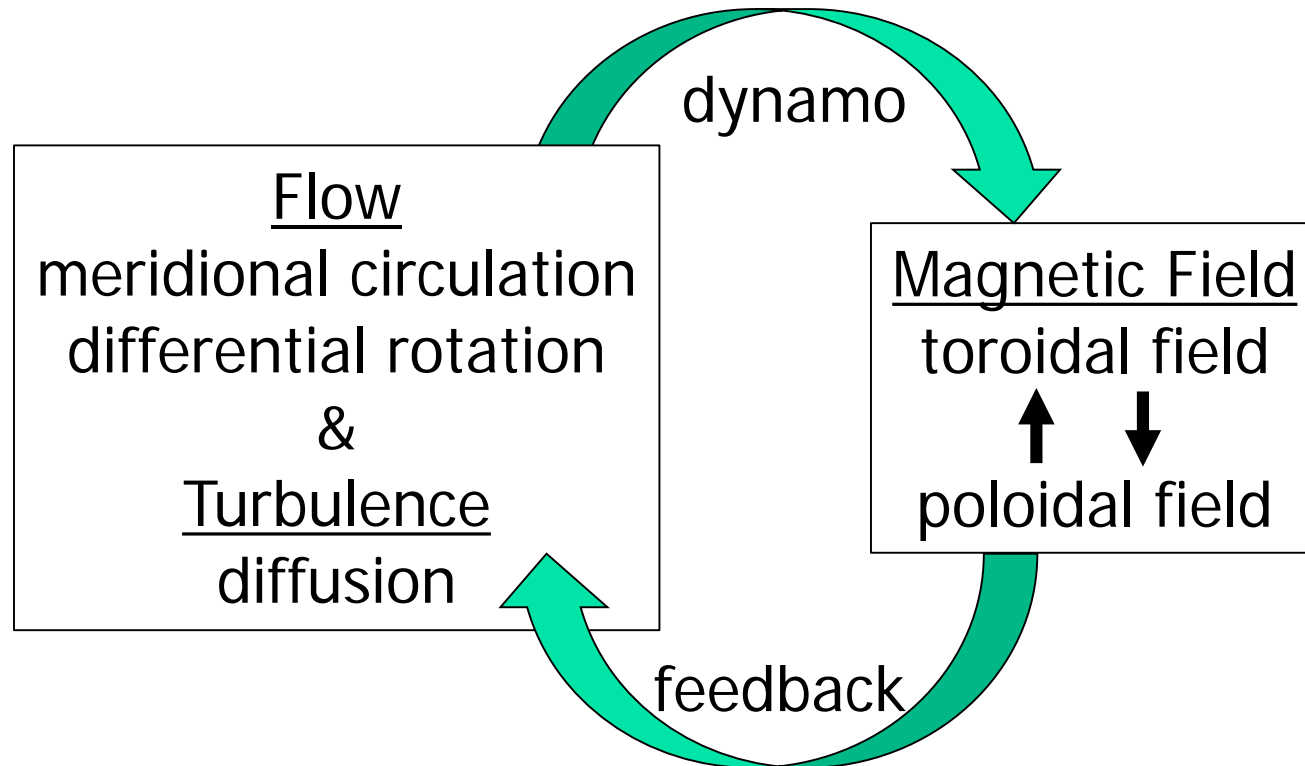
# 3D MHD Simulation

- Passos & Charbonneau 2014
- Norton, Charbonneau & Passos 2014



The N-S asymmetry is spontaneously generated, but the lag of cycle phase seems to execute a form of random walk rather than the trend of long-term persistence.

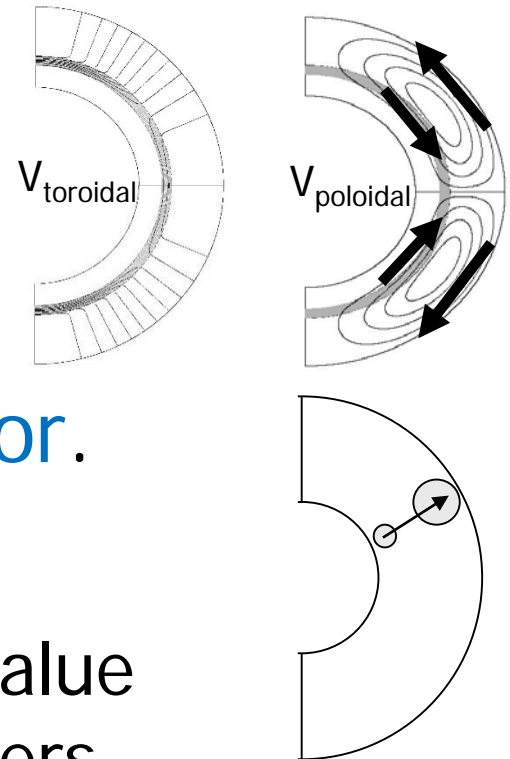
# What is the cause of asymmetry?



**Objective of our study:** To find the **minimal model** to explain the N-S asymmetry of solar cycle.

# Simulation model

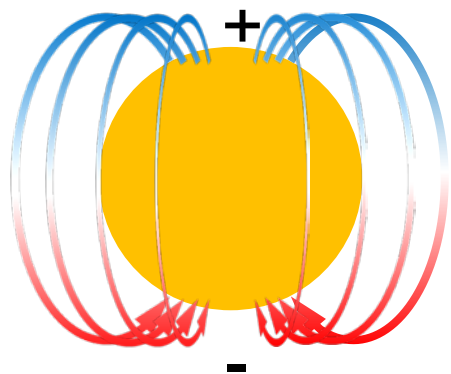
- **Algorithm:** Same as SURYA code (Chatterjee, Nandy, and Choudhuri 2004).
- **Geometry:** 2D (axisymmetric) full spherical shell.
- **Dynamo model:**  $\alpha\Omega$ -dynamo with differential rotation and meridional circulation, those are symmetric with respect to equator.
- **Magnetic buoyancy effect:**
  - Toroidal field exceeding a critical value is made to erupt to the surface layers.



# Parity of Dynamo

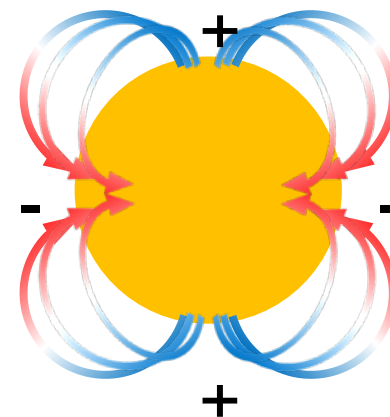
Ref. Jennings & Weiss (1991)

Nishikawa and Kusano (2008)



$$(B_r^a, B_\theta^s, B_\phi^a)$$

**Dipole-type**



$$(B_r^s, B_\theta^a, B_\phi^s)$$

**Quadrupole-type**

$$B_\phi^s(\theta) \equiv [B_\phi(\theta) + B_\phi(\pi - \theta)] / 2$$

$$B_\phi^a(\theta) \equiv [B_\phi(\theta) - B_\phi(\pi - \theta)] / 2$$



# Equations

quadrupole  
type

$$\begin{aligned} \frac{\partial B_\phi^s}{\partial t} + s \mathbf{v}_p^s \cdot \nabla \left( \frac{B_\phi^s}{s} \right) + B_\phi^s \nabla \cdot \mathbf{v}_p^s \\ = \eta_t \left( \nabla^2 - \frac{1}{s^2} \right) B_\phi^s + \frac{1}{r} \frac{d\eta_t}{dr} \frac{\partial}{\partial r} (r B_\phi^s) + s (\mathbf{B}_p^s \cdot \nabla) \Omega^s \end{aligned}$$

$$\frac{\partial A_\phi^a}{\partial t} + \frac{1}{s} (\mathbf{v}_p^s \cdot \nabla) (s A_\phi^a) = \eta_p \left( \nabla^2 - \frac{1}{s^2} \right) A_\phi^a + \alpha B_\phi^s$$

Magnetic buoyancy effect

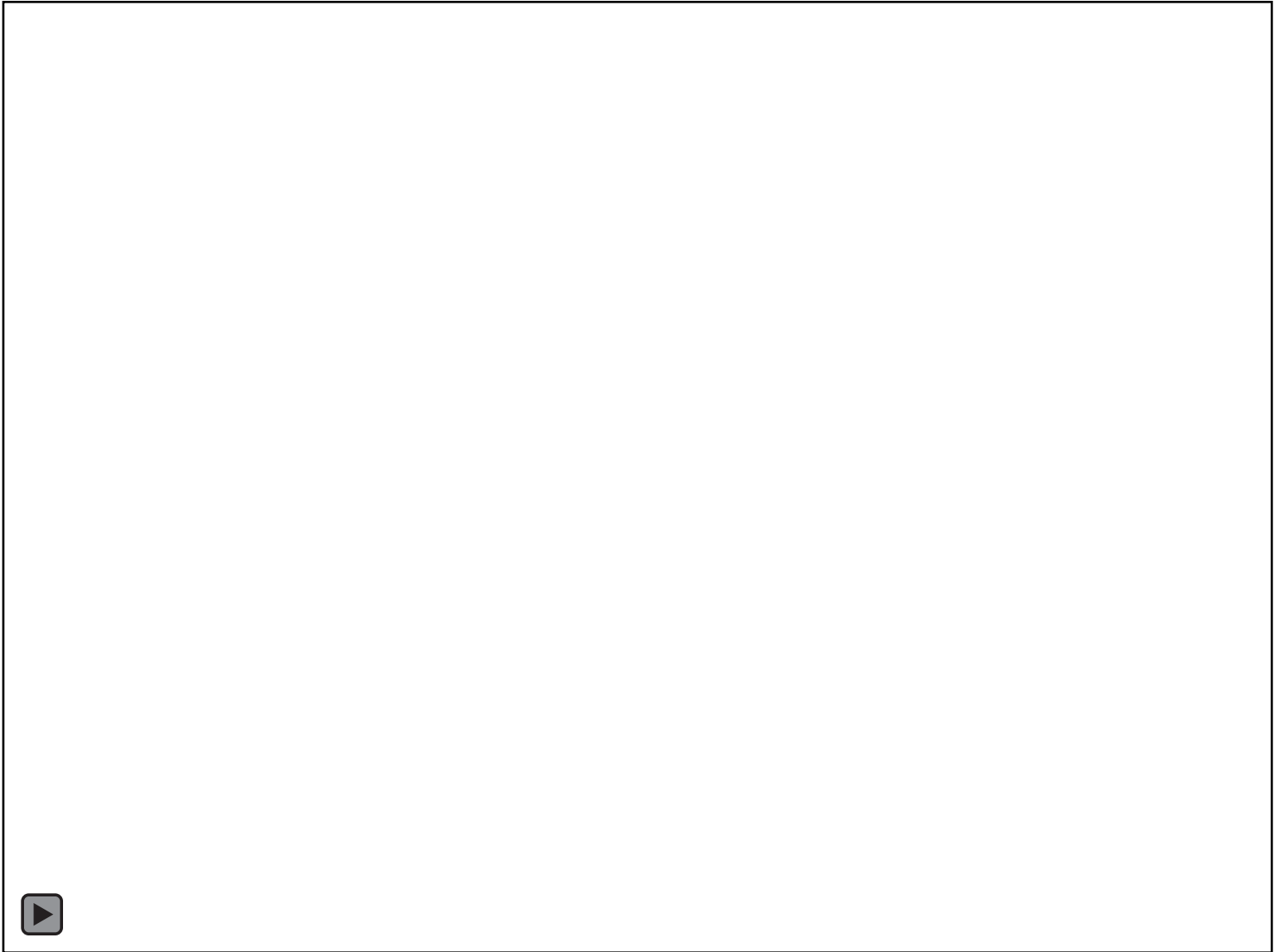
dipole  
type

$$\begin{aligned} \frac{\partial B_\phi^a}{\partial t} + s \mathbf{v}_p^s \cdot \nabla \left( \frac{B_\phi^a}{s} \right) + B_\phi^a \nabla \cdot \mathbf{v}_p^s \\ = \eta_t \left( \nabla^2 - \frac{1}{s^2} \right) B_\phi^a + \frac{1}{r} \frac{d\eta_t}{dr} \frac{\partial}{\partial r} (r B_\phi^a) + s (\mathbf{B}_p^a \cdot \nabla) \Omega^s \end{aligned}$$

$$\frac{\partial A_\phi^s}{\partial t} + \frac{1}{s} (\mathbf{v}_p^s \cdot \nabla) (s A_\phi^s) = \eta_p \left( \nabla^2 - \frac{1}{s^2} \right) A_\phi^s + \alpha B_\phi^a$$

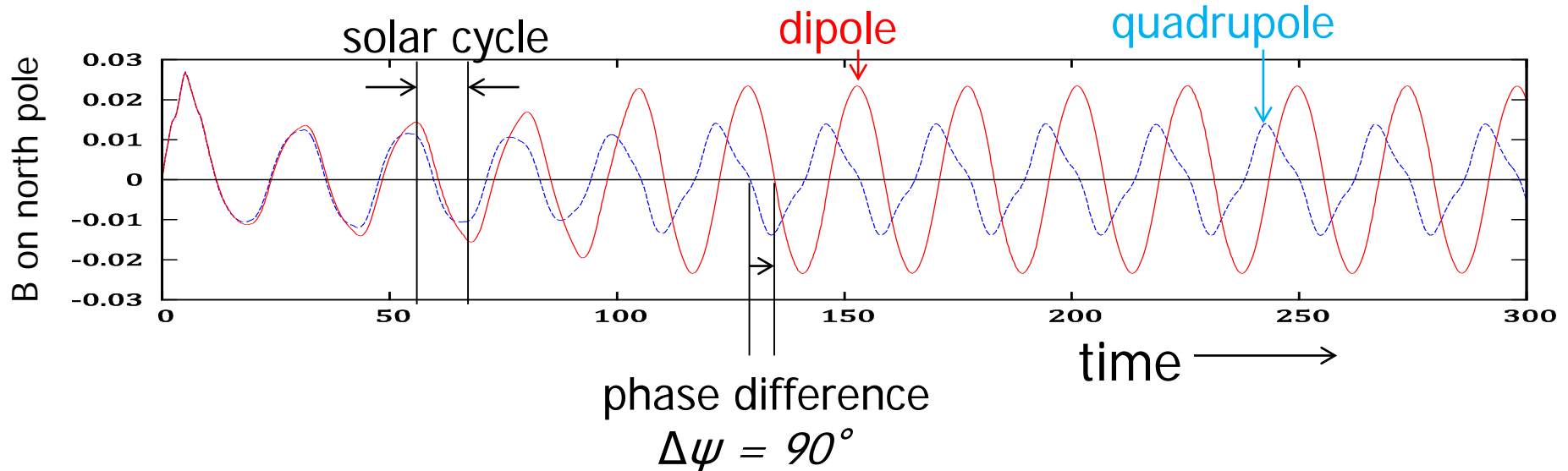
# Result

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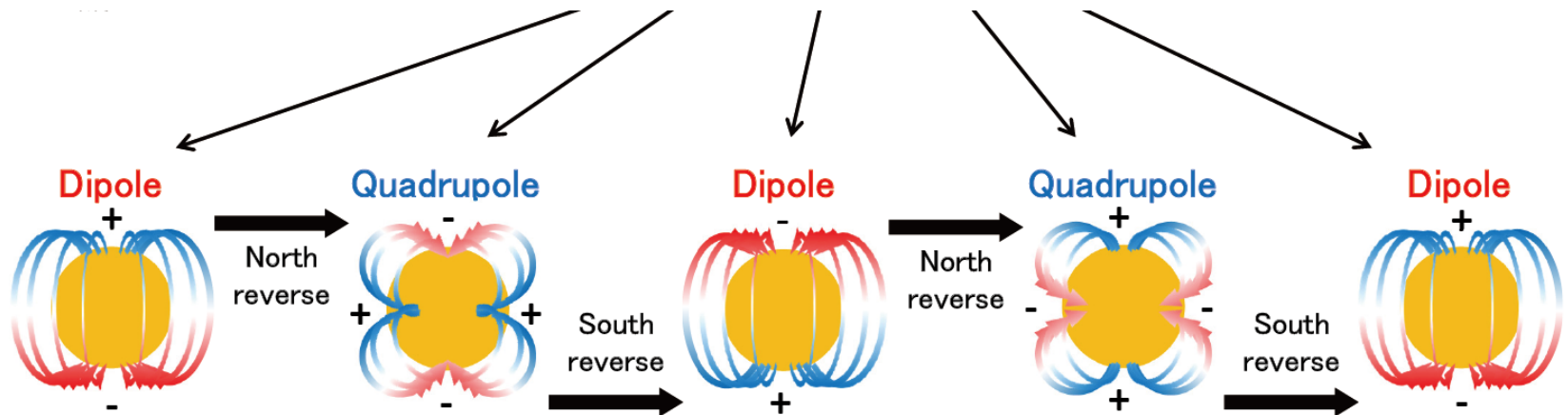
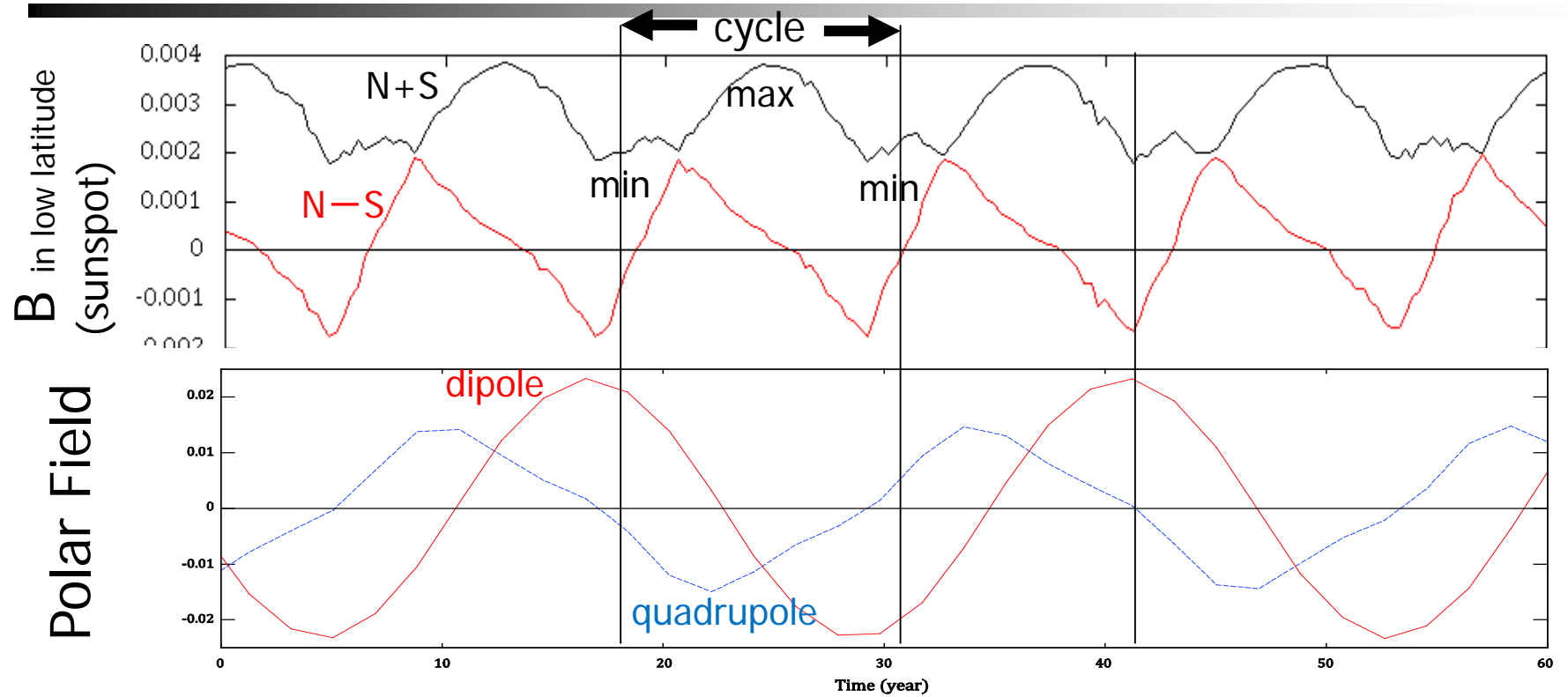
# Result

- The cyclic oscillation of polar magnetic field

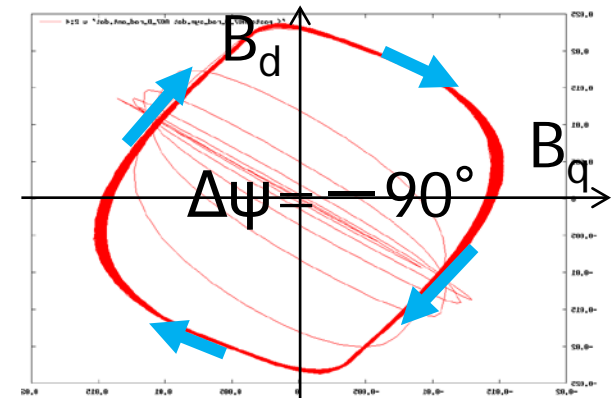
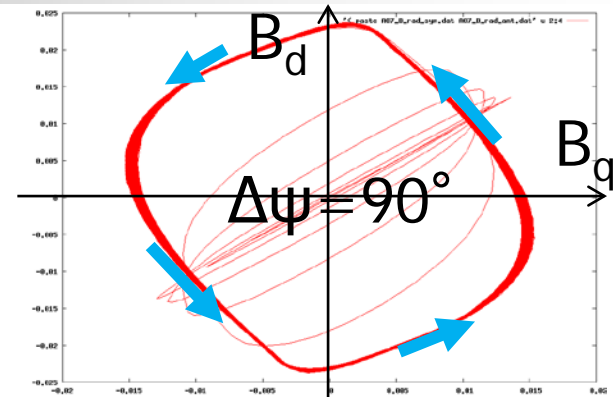
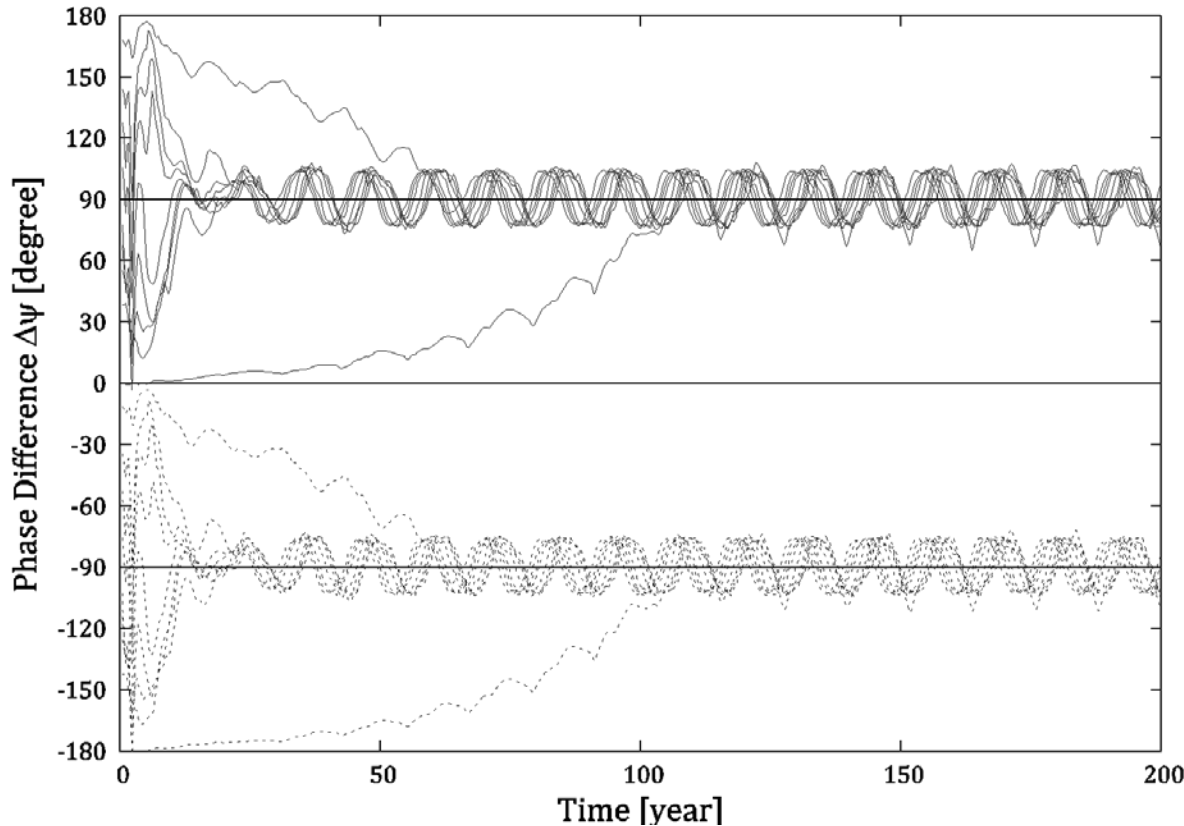


- Both the dipole and quadrupole-type fields oscillates with the same period corresponding to the double solar cycle.
- The phase difference b/w the two components spontaneously shifts to  $90^\circ$  and then is persistent.

# Solar Cycle for $\Delta\psi=90^\circ$



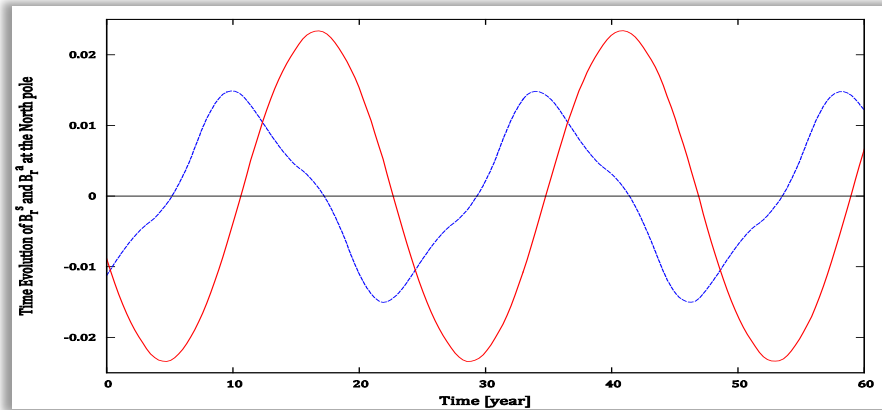
# Dependency on the Initial Phase



- Regardless of the initial condition, the phase difference  $\Delta\psi$  always falls into  $90^\circ$  or  $-90^\circ$ .
- They correspond to **two attractors**.

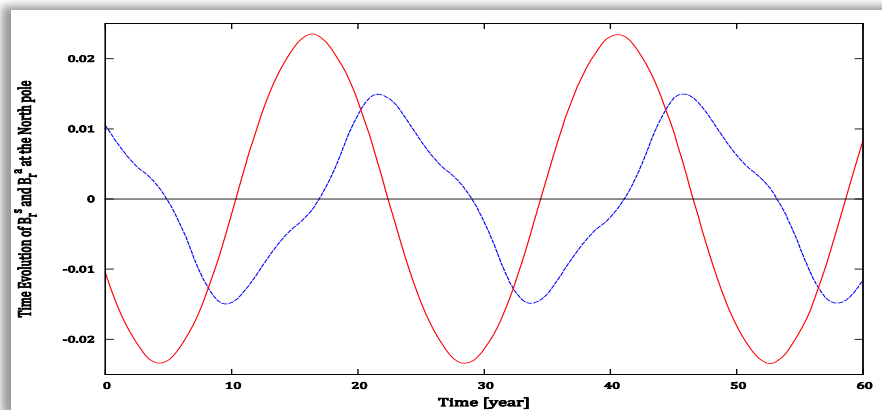


# Properties of the Two Attractors



The attractor for  $\Delta\psi=90^\circ$

Sunspot in the north is more active in the early phase and the polar field in the north is first reversed.

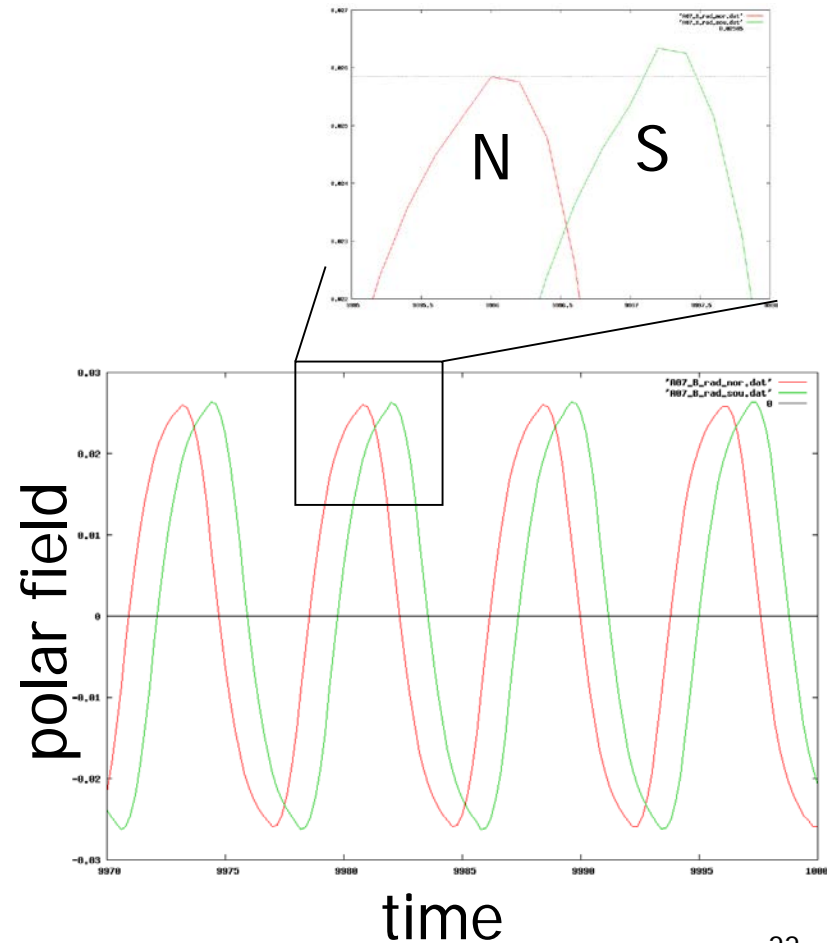
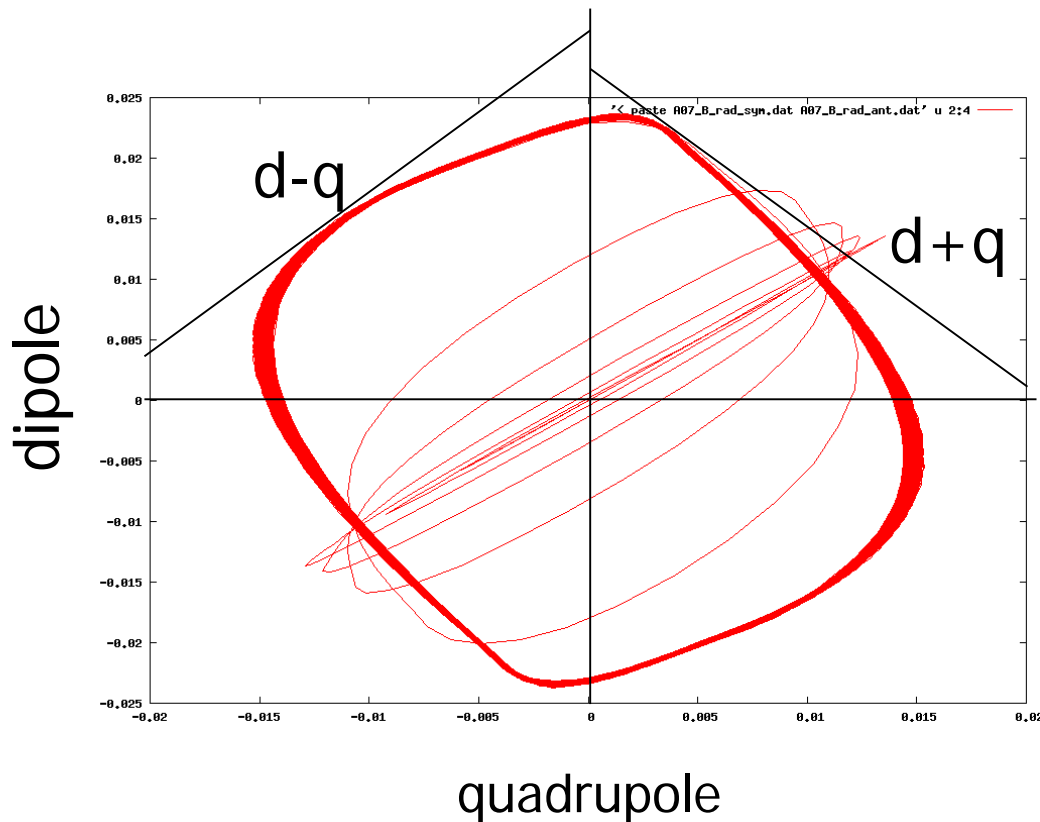


The attractor for  $\Delta\psi=-90^\circ$

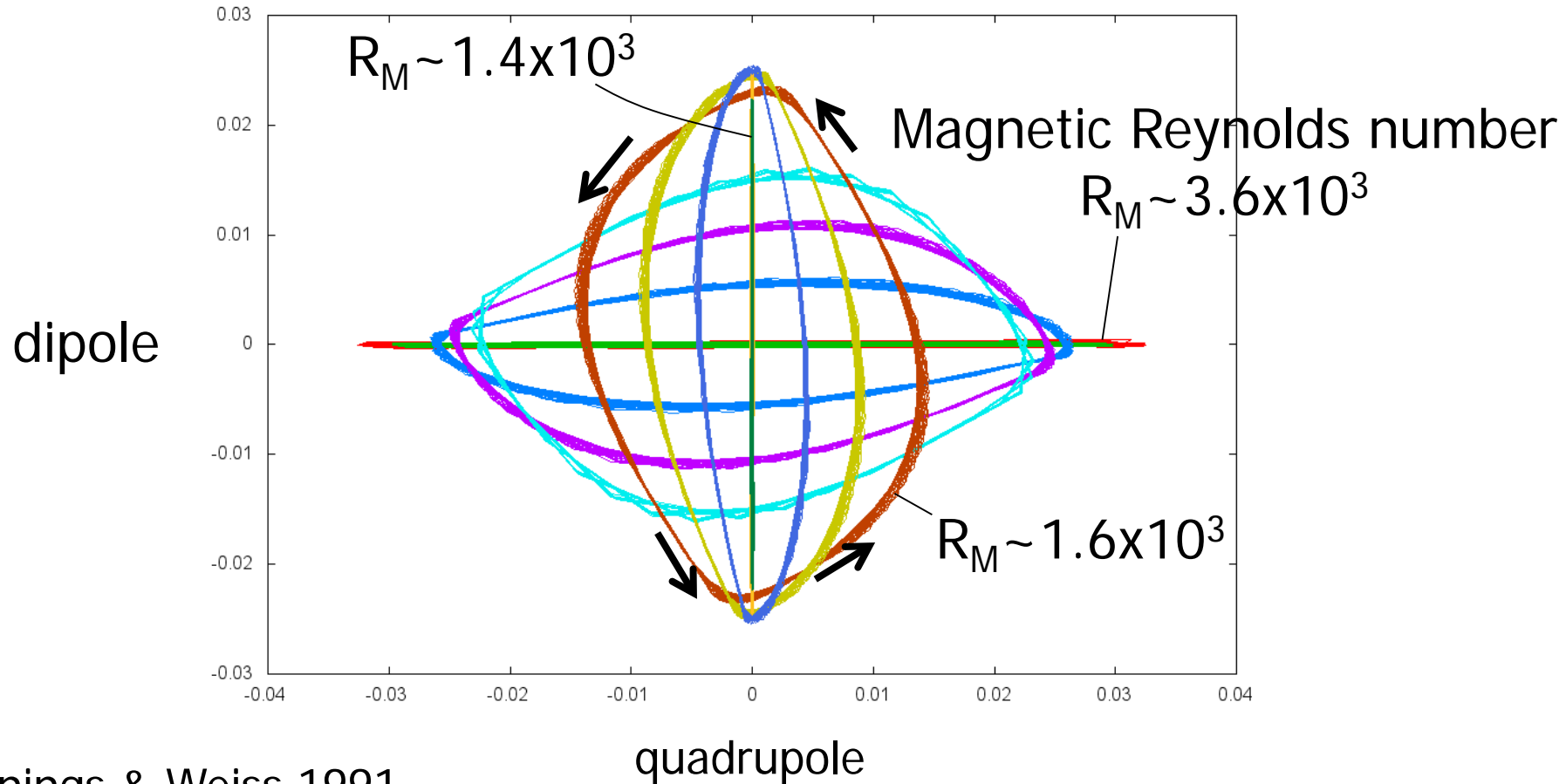
Sunspot in the south is more active in the early phase and the polar field in the south is first reversed.

# Asymmetry in polar field intensity

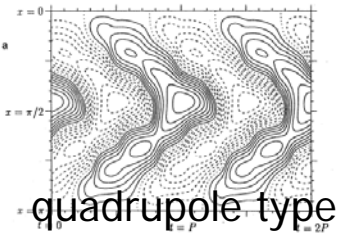
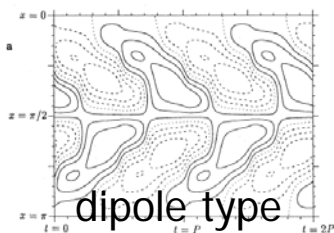
- The squashed factor of attractor causes the difference of polar field max intensity between the north and south pole



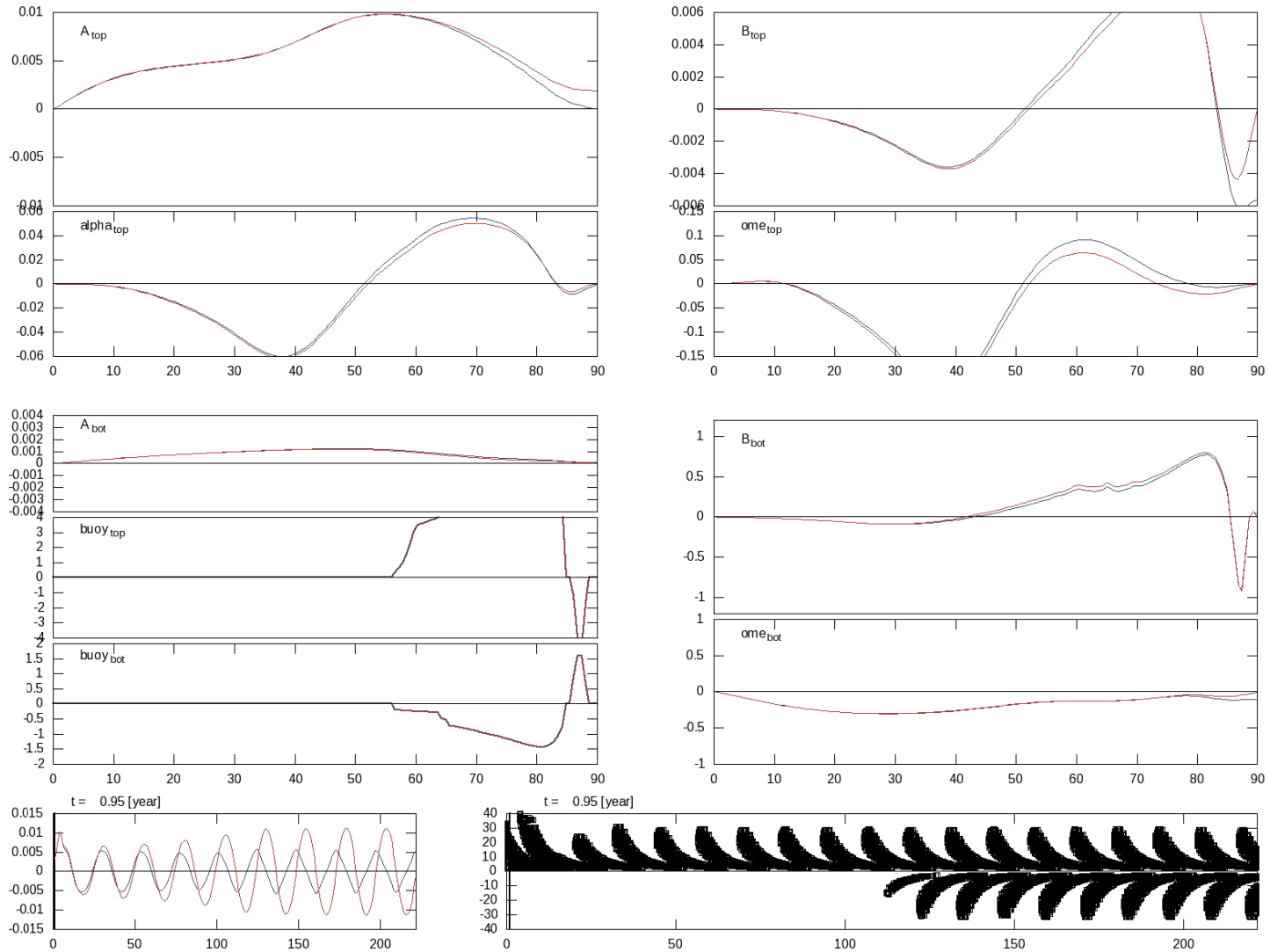
# Dependency of attractors on $R_M$



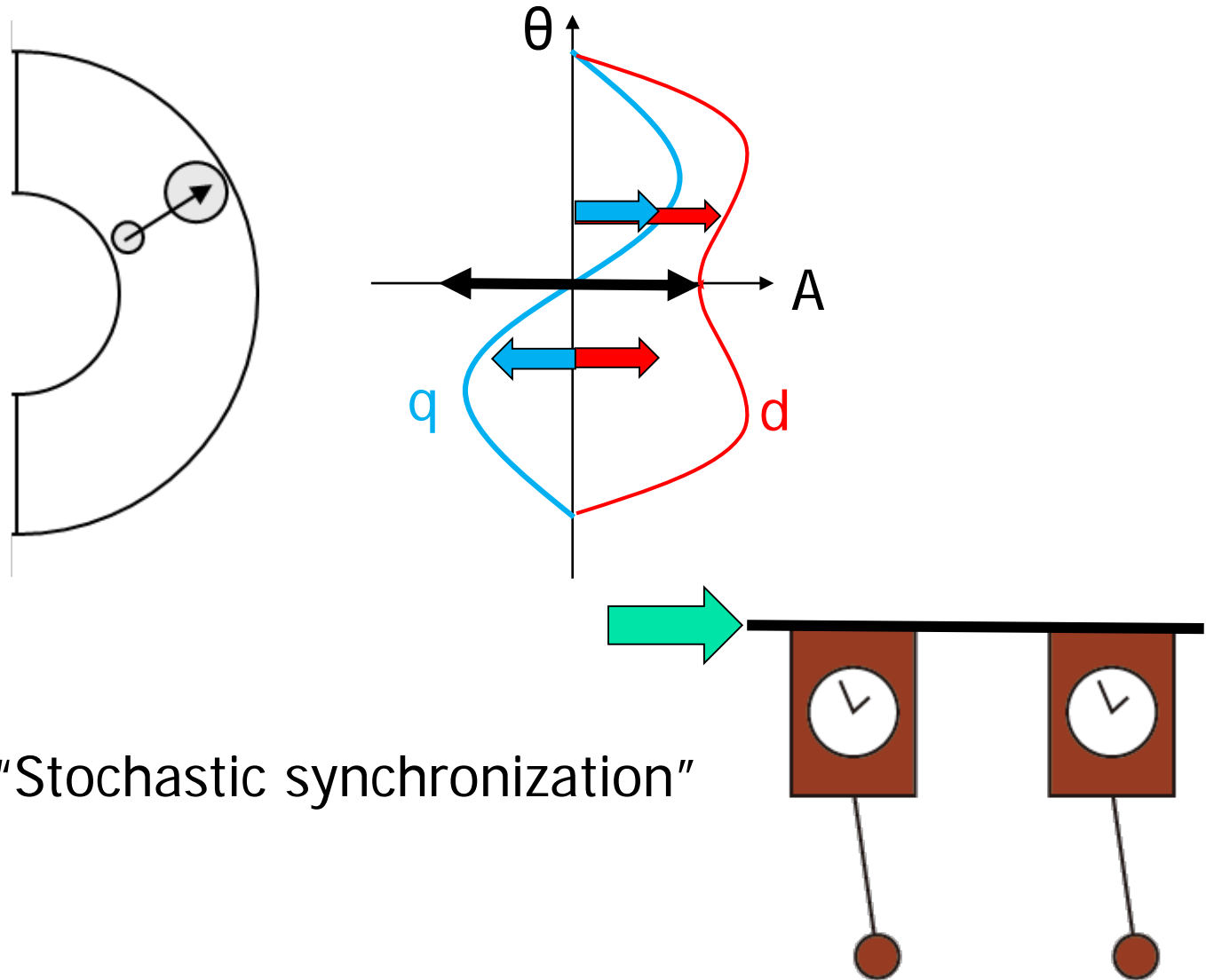
Jennings & Weiss 1991



# Why attractors for $\Delta\psi = \pm 90^\circ$



# Mechanism of attractors





# Summary

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- The flux transport dynamo model **well explains the asymmetric reversal of polar field** as well as the lag of solar cycle between the N-S hemisphere, even if the flow is symmetric.
- There are **two attractors** in which the dipole and quadrupole field coexist and the phases are shifted (+ or -) 90 degrees.
- It means that the asymmetry of spherical dynamo can be inherently generated.
- However, the simple flux transport model cannot reproduce the transition b/w the different attractors, which corresponds to the switch of different hemispheric parity (NS $\leftrightarrow$ SN).